

Low-energy collisions between electrons and BeH⁺: cross sections and rate coefficients for all the vibrational states of the ion

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Abstract

We provide cross sections and Maxwell rate coefficients for reactive collisions of slow electrons with BeH⁺ ions on all the eighteen vibrational levels ($X^1\Sigma^+, v_i^+ = 0, 1, 2, \dots, 17$) using a Multichannel Quantum Defect Theory (MQDT) - type approach. These data on dissociative recombination, vibrational excitation and vibrational de-excitation are relevant for magnetic confinement fusion edge plasma modelling and spectroscopy, in devices with beryllium based main chamber materials, such as the International Thermonuclear Experimental Reactor (ITER) and the Joint European Torus (JET). Our results are presented in graphical form and as fitted analytical functions, the parameters of which are organized in tables.

Keywords: Plasma-wall interaction; electron-impact processes; multi-channel; dissociative recombination; vibrational excitation; cross sections and rates.

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1. Introduction

Even though various isotopes of light elements can be coupled to achieve thermonuclear fusion energy release, the next generation of thermonuclear fusion reactors will use deuterium-tritium (D-T) reactions, by far most efficient and accessible plasma fuel for fusion reactors and power plants. As discussed in detail elsewhere [1, 2, 3, 4, 5, 6], beryllium (Be) is meant to enter the composition of the wall of the future fusion devices (ITER). Its performance on preventing tritium retention and, meanwhile, still keeping the benefits of a low Z material (low fuel dilution), is currently being tested in the JET [3, 4]. According to current plans, tungsten (W) will be the plasma facing material in the high heat flux components (the entire divertor). These materials (Be and W) are expected to provide sufficiently low fuel retention, plasma impurity levels, neutron damage, and sufficient heat removal capabilities in the divertor and then, meet ITER requirements [2]. The key challenge in the use of beryllium as main chamber material for experimental and commercial fusion devices is to understand, predict and control the characteristics of the thermonuclear burning plasma, the plasma edge regimes that result in acceptable erosion performance and the divertor plasma (heat and particle exhaust, impurity control, lifetime).

Due to the low mass ratio between beryllium and the D, T plasma fuel ions, beryllium erodes rather easily under plasma exposure by physical and chemical sputtering, a process which releases Be, Be^+ , and other impurities into the plasma. Significant fractions of the eroded beryllium will be transported towards the divertor and will form compounds with the fuel atoms, molecules and/or molecular ions. Therefore, BeH as well as BeD and BeT molecules are expected to appear in a significant (spectroscopically detectable) amount in the edge and divertor plasmas. Various source mechanisms may lead to their formation, either surface or volumetric (particle rearrangement) processes. The particle interchange reaction [7],

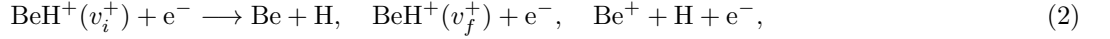


where X denotes one of the fuel atoms H, D or T, was suggested as one, possibly dominant, volumetric BeX formation channel, when X_2 is in its vibrational ground state. However, the exo- or endothermicity will greatly depend upon the vibrational state of X_2 and other channels, including electron transfer channels, may also be open for BeX formation in fusion divertor plasma conditions. The involved particles - atoms, molecules and molecular ions - follow their often quite complex transport pathways in the edge plasma and take part in the complex reactions determining the plasma composition. Its detailed modeling by taking into account reactions between all present species is necessary, first of all, for interpretation of molecular and atomic line spectroscopy and also to understand and predict the overall plasma edge dynamics and the divertor region behavior in particular.

In principle, the rate of beryllium erosion in fusion devices can be measured by spectroscopical techniques of all the states of the atoms and molecules, so primarily of Be, Be^+ , Be_2^+ , BeX, BeX^+ , BeX_2 , BeX_2^+ . In order to provide a quantitative interpretation of such spectroscopic measurements, one needs a complete set of rate coefficients for excitation, ionization and the various atomic and molecular ions break-up reactions. The inelastic electron-impact processes of vibrationally excited beryllium monohydride BeH^+ play a key role in the reaction kinetics of low-temperature plasmas in general, and potentially also in certain cold regions of fusion reactor relevant (e.g. the divertor) plasmas. In order to model and diagnose plasmas containing BeH^+ it is essential to build a complete database of cross-sections and rate coefficients for electron-impact collision processes. Knowing the loss rates of BeH^+ (and isotopologues) as well as

absolutely calibrated spectroscopic emission from this molecular ion will allow to draw conclusions also about the BeH^+ formation rates.

The BeH^+ ion is subject to Dissociative Recombination (DR), competed by Vibrational Transitions (VT) - excitation/de-excitation (VE/VdE) - and Dissociative Excitation (DE) respectively [8]:



$(v_i^+)/(v_f^+)$ standing for the initial/final vibrational levels of the cation.

Whereas for numerous ions measurements of these reactive collisions have been performed in magnetostatic or electrostatic storage rings (multipass experiments using merged electron and ion beams) [8], this is certainly not the case for BeH^+ , beryllium being highly toxic.

In the current study, we performed large scale computations of cross sections for the reactive collisions DR, VE and VdE displayed in eq. (2), as well as of the corresponding rate coefficients.

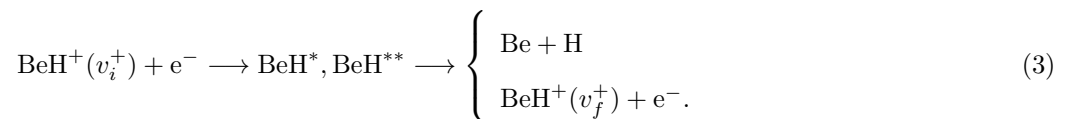
More specifically, we have used the molecular structure data computed by some of us [9] in order to model the dynamics of these reactions by our stepwise MQDT-method, neglecting the rotational structure and interactions [10, 11, 12, 13]. Whereas our previous works [9, 13] restricted to the ground and three lowest vibrationally-excited levels of BeH^+ , we have extended here our analysis to the whole range of its vibrational states, i.e. up to $v_i^+ = 17$.

After briefly reminding the major ideas and steps of our MQDT method, including the main features and parameters of the computational part (section 2), we present the cross sections and rate coefficients below 2.7 eV - dissociation threshold - and below 5000 K respectively (section 3). The coefficients appearing in the analytical functions used to fit the rate coefficients are organized in tables.

At higher energy of the incident electron, a further competing process, dissociation excitation, will become effective. The collisional data for this range are the subject of ongoing calculations.

2. Theoretical approach of the dynamics

In this paper, we use an MQDT-type method to study the electron-impact collision processes:



resulting from the quantum interference between the *direct* mechanism - involving the doubly excited resonant states BeH^{**} - and the *indirect* one - occurring via Rydberg singly-excited predissociating states BeH^* .

A detailed description of our theoretical approach was given in [13]. Its main steps are the following:

i) Building of the interaction matrix \mathcal{V} : It is based on the computed [9, 13] Rydberg-valence couplings within a quasi-diabatic representation of molecular states of the neutral system. The matrix elements of this matrix correspond to - and are accordingly indexed with - all the possible pairs of channels. More specifically, for a given electronic total angular momentum quantum number Λ and a given symmetry (total electronic spin singlet/triplet) of the neutral, our formalism rely on *ionization* channels - labelled by the vibrational quantum number of the cation v^+ and the orbital quantum number l of the incident/Rydberg electron - and on *dissociation* channels labelled d_j .

ii) *Computation of the reaction matrix \mathcal{K}* : it is performed by adopting for the Lippman-Schwinger integral equation the second-order perturbative solution [14, 15, 16], written in operatorial form as:

$$\mathcal{K} = \mathcal{V} + \mathcal{V} \frac{1}{E - \mathbf{H}_0} \mathcal{V}, \quad (4)$$

\mathbf{H}_0 being the Hamiltonian of the molecular system under study in which the Rydberg-valence interaction is neglected.

iii) *Computation of the eigenchannel wavefunctions*: It relies on the eigenvectors and eigenvalues of the reaction matrix \mathcal{K} , i.e. the columns of the matrix \mathbf{U} and the elements of the diagonal matrix $\mathbf{tan}(\boldsymbol{\eta})$ respectively :

$$\mathcal{K}\mathbf{U} = -\frac{1}{\pi} \mathbf{tan}(\boldsymbol{\eta})\mathbf{U} \quad (5)$$

where the non-vanishing elements of the diagonal matrix $\boldsymbol{\eta}$ are the phaseshifts introduced into the wavefunctions by the short-range interactions.

iv) *Frame transformation from the Born-Oppenheimer representation to the close-coupling one*: It is performed via the matrices \mathcal{C} and \mathcal{S} , built on the basis of the matrices \mathbf{U} and $\boldsymbol{\eta}$ and on the quantum defect characterizing the incident/Rydberg electron, $\mu_l^\Lambda(R)$.

v) *Construction of the generalized scattering matrix \mathcal{X}* , eventually split in blocks associated to open and/or closed (o and/or c respectively) channels:

$$\mathcal{X} = \frac{\mathcal{C} + i\mathcal{S}}{\mathcal{C} - i\mathcal{S}} \quad \mathcal{X} = \begin{pmatrix} X_{oo} & X_{oc} \\ X_{co} & X_{cc} \end{pmatrix}. \quad (6)$$

vi) *Construction of the physical scattering matrix \mathcal{S}* , whose elements link mutually the open channels exclusively, given by [17]:

$$\mathcal{S} = X_{oo} - X_{oc} \frac{1}{X_{cc} - \exp(-i2\pi\boldsymbol{\nu})} X_{co}. \quad (7)$$

Here the matrix $\exp(-i2\pi\boldsymbol{\nu})$ is diagonal and relies on the effective quantum numbers ν_{v+} associated to the vibrational thresholds of the closed channels.

vii) *Computation of the cross-sections*: Given the target cation on its level v_i^+ , its impact with an electron of energy ε results either in dissociative recombination or in vibrational excitation/de-excitation according to the formulae:

$$\sigma_{\text{diss} \leftarrow v_i^+} = \sum_{\Lambda, \text{sym}} \sigma_{\text{diss} \leftarrow v_i^+}^{\text{sym}, \Lambda}, \quad \sigma_{\text{diss} \leftarrow v_i^+}^{\text{sym}, \Lambda} = \frac{\pi}{4\varepsilon} \rho^{\text{sym}, \Lambda} \sum_{l, j} |S_{d_j, lv_i^+}|^2, \quad (8)$$

$$\sigma_{v_f^+ \leftarrow v_i^+} = \sum_{\Lambda, \text{sym}} \sigma_{v_f^+ \leftarrow v_i^+}^{\text{sym}, \Lambda}, \quad \sigma_{v_f^+ \leftarrow v_i^+}^{\text{sym}, \Lambda} = \frac{\pi}{4\varepsilon} \rho^{\text{sym}, \Lambda} \sum_{l, l'} |S_{l'v_f^+, lv_i^+} - \delta_{l'l} \delta_{v_i^+ v_f^+}|^2, \quad (9)$$

where, $\rho^{\text{sym}, \Lambda}$ stands for the ratio between the multiplicity of the involved electronic states of BeH and that of the target, BeH⁺.

3. Results

Using the available molecular data - quasi-diabatic potential energy curves and electronic couplings for ²Π, ²Σ⁺ and ²Δ states displayed in Figure 1 of [13] (for more details see as well [9, 18]) - we have extended our previous calculations

- initially restricted to the ground and weakly excited vibrational states - to *all* vibrational levels (up to $v_i^+ = 17$) of the ground electronic state. The energy of the electron is inferior to 2.7 eV, this value corresponding to the dissociation threshold of the ground state ion.

In all the panels of graphs 1-6, the vertical green lines mark the energy or the temperature below which the calculations are the most accurate. Indeed, above these thresholds, these calculations neglect the role of the dissociative excitation of the ion. Nevertheless, the data displayed continue to be reasonably correct above the thresholds because this process weakly affects the DR and the VT at low energy/temperature.

In order to illustrate the vibrational dependence of the dissociative recombination and to compare the two mechanisms - direct and total - we display in Graphs 1, 2, and 3 the corresponding cross sections. One may notice that the total (direct *coherently* added to indirect) cross section is characterized by resonant captures into Rydberg states, but that they do not contribute too much in average.

Similar features characterize the cross sections of competitive processes, VE and VdE, but we do not display them here, restricting ourselves to show only their Maxwell rate coefficients.

Indeed, graphs 4, 5, and 6 give the whole ensemble of rate coefficients available for the state-to-state kinetics of BeH^+ . They illustrate the dominance of the DR in its $v_i^+ = 0 - 9$ levels at low electronic temperature, while the VdE becomes more important than the other processes for initial vibrational states $v_i^+ > 9$.

Graph 7 provides the comparison between the DR rate coefficients and the *global* - i.e. coming from the sum over all the possible final levels - vibrational transitions rate coefficients. One may notice that the excitation process becomes a notable competitor to DR and VdE above 1000 K only.

In order to allow the versatile implementation of the rate coefficients shown in Graph 4-6 in kinetics modelling codes, we have fitted them with generalized Arrhenius-type formulas:

$$k_{(\text{BeH}^+, L)}^P(T_e) = A_L T_e^{\alpha_L} \exp \left[- \sum_{j=1}^7 \frac{B_L(j)}{j T_e^j} \right], \quad (10)$$

over the electron temperature range $100 \text{ K} \leq T_e \leq 5000 \text{ K}$, 'P' and 'L' standing for Processes (DR or VT) and Levels (v_i^+ or $v_i^+ \rightarrow v_f^+$) respectively. The coefficients for Dissociative Recombination (when P corresponds to DR) $A_{v_i^+}$, $\alpha_{v_i^+}$ and $B_{v_i^+}(j)$ are displayed in Table 1, and those for Vibrational Transitions (when P corresponds to VT, i.e. VE and VdE) $A_{v_i^+ \rightarrow v_f^+}$, $\alpha_{v_i^+ \rightarrow v_f^+}$ and $B_{v_i^+ \rightarrow v_f^+}(j)$ are given in Tables 2-10. The values interpolated using the equation (10) agree with the MQDT-computed ones within a few percent, and are represented in Graphs 4-6.

4. Conclusions

The present paper provides a complete state-to-state information of the BeH^+ reactive collisions with electrons, illustrating quantitatively the competition between the vibrational transitions and dissociative recombination. We display the cross sections or/and the Maxwell rate coefficients for the molecular ion in all of its initial vibrational states and for the entire range of energies of the incident electron below the ion dissociation threshold.

Arrhenius-type formulas are used in order to fit the rate coefficients as function of T_e , the electronic temperature. These rate coefficients strongly depend on the initial vibrational level of the molecular ion.

These data are addressed to the fusion community - being relevant to the modeling of the edge of the fusion plasma as well as for divertor conditions - and, more generally, to the modelers of any beryllium-containing-plasmas, produced in laboratory experiments, industrial processing and natural environments. No experimental work concerning the electron/BeH⁺ collisions can be found in the literature.

Further studies, devoted to higher energy and consequently taking into account the dissociative excitation [19], as well as others, extending to isotopomers of BeH⁺ (BeD⁺, BeT⁺) are the object of ongoing work. All these data, as well as the presently displayed ones will be of huge importance for modeling of the plasma/wall interaction [3].

Acknowledgments

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Explanation of Graphs

Graph 1-3. Dissociative recombination cross sections for all the vibrational levels of BeH^+ in its ground electronic state.

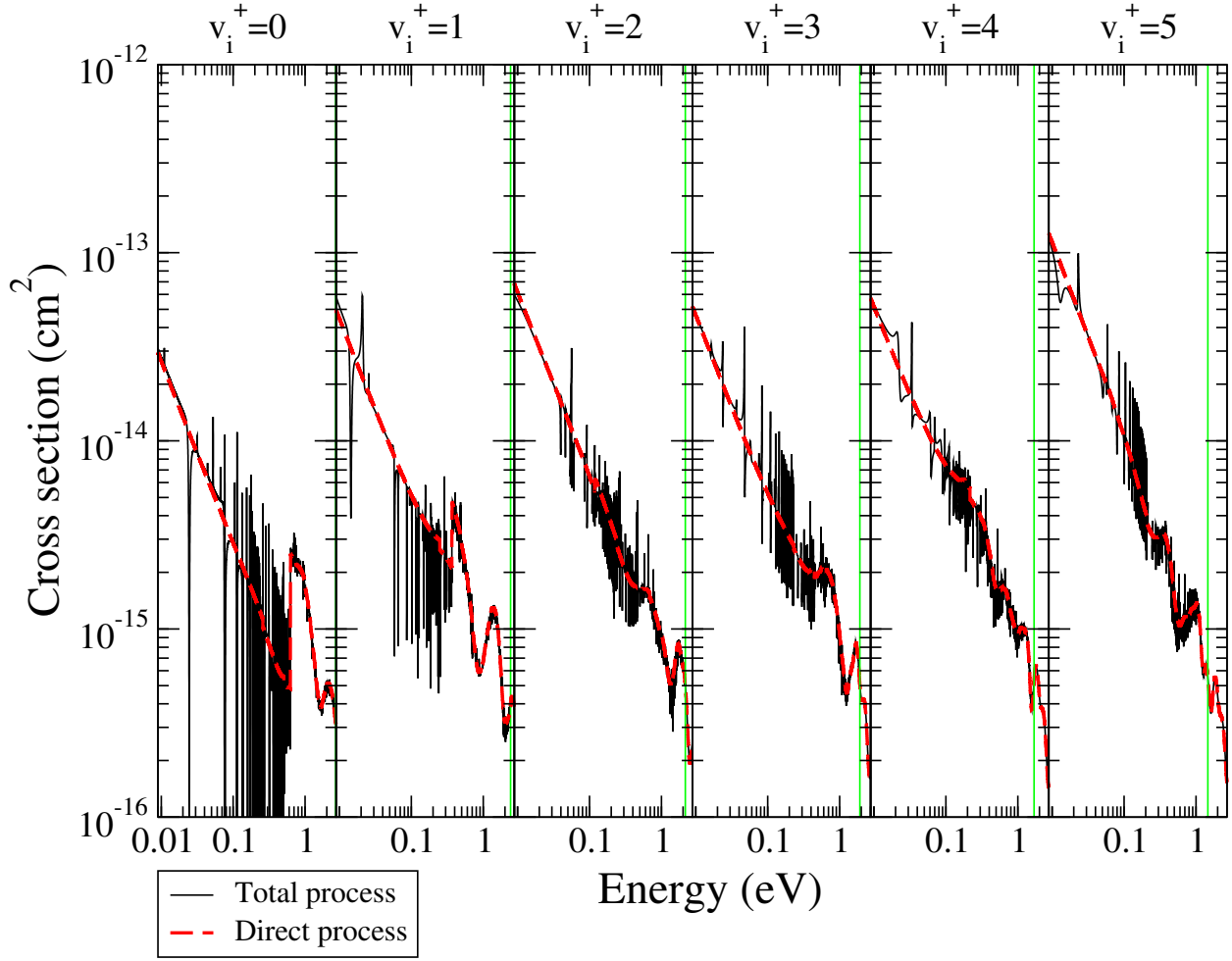
Ordinate	Cross section in cm^2
Abscissa	Collision (electron) energy in eV
Black solid line	Total (direct and indirect) process
Red dashed line	Direct process
Green vertical line	Precision limit, for details see the text

Graph 4-6. Dissociative recombination, vibrational excitation and de-excitation Maxwell rate coefficients for all the vibrational levels of BeH^+ in its ground electronic state.

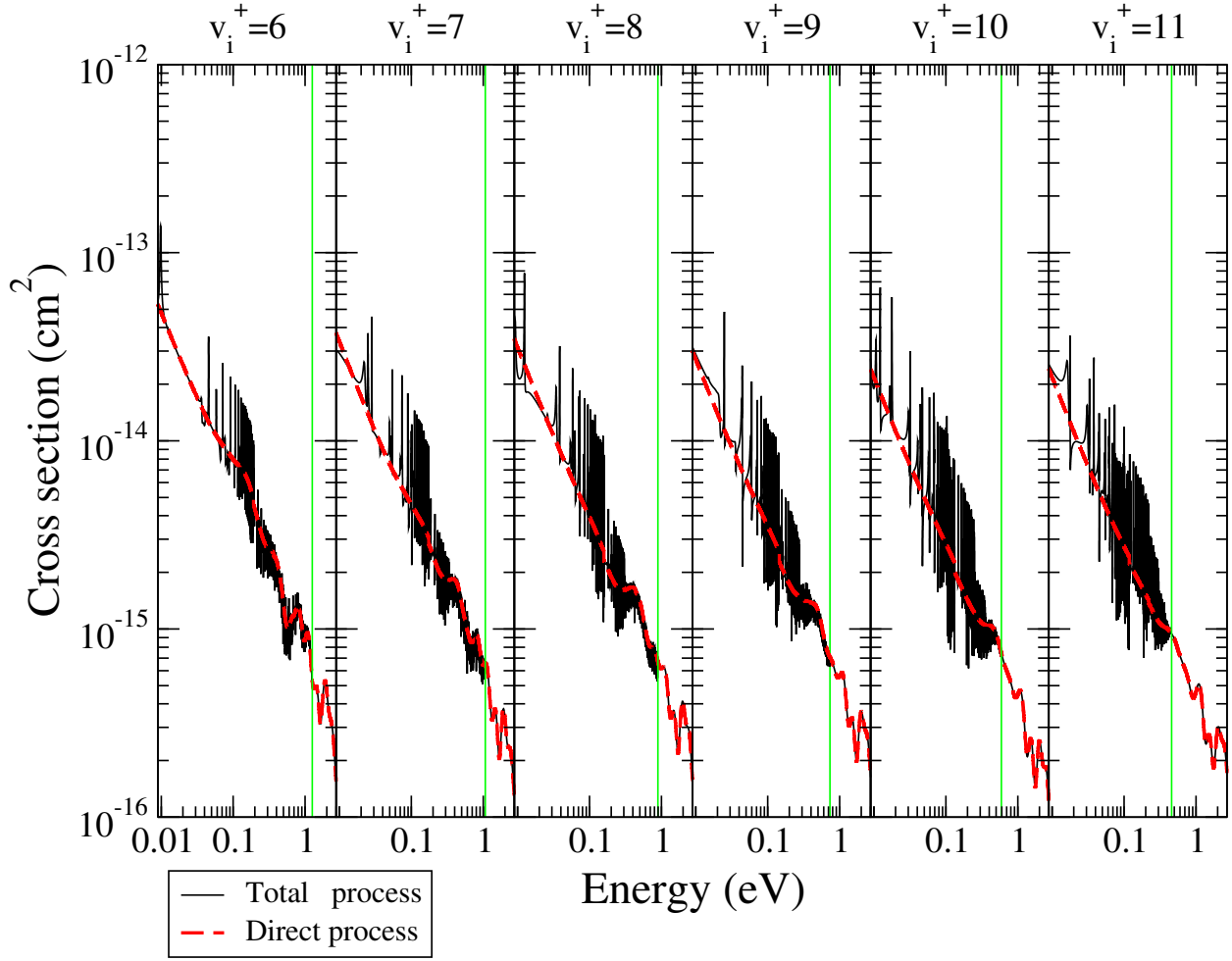
Ordinate	Maxwell rate coefficient in $\text{cm}^3 \cdot \text{s}^{-1}$
Abscissa	Electron temperature in K
Thick black line	DR Maxwell rate coefficient
Thin coloured lines	Vibrational excitation rate coefficients
Coloured lines with symbols	Vibrational de-excitation rate coefficients
Green vertical line	Precision limit, for details see the text

Graph 7. Global (summed-up for all possible final states) dissociative recombination, vibrational excitation and de-excitation Maxwell rate coefficients for BeH^+ in its ground electronic state.

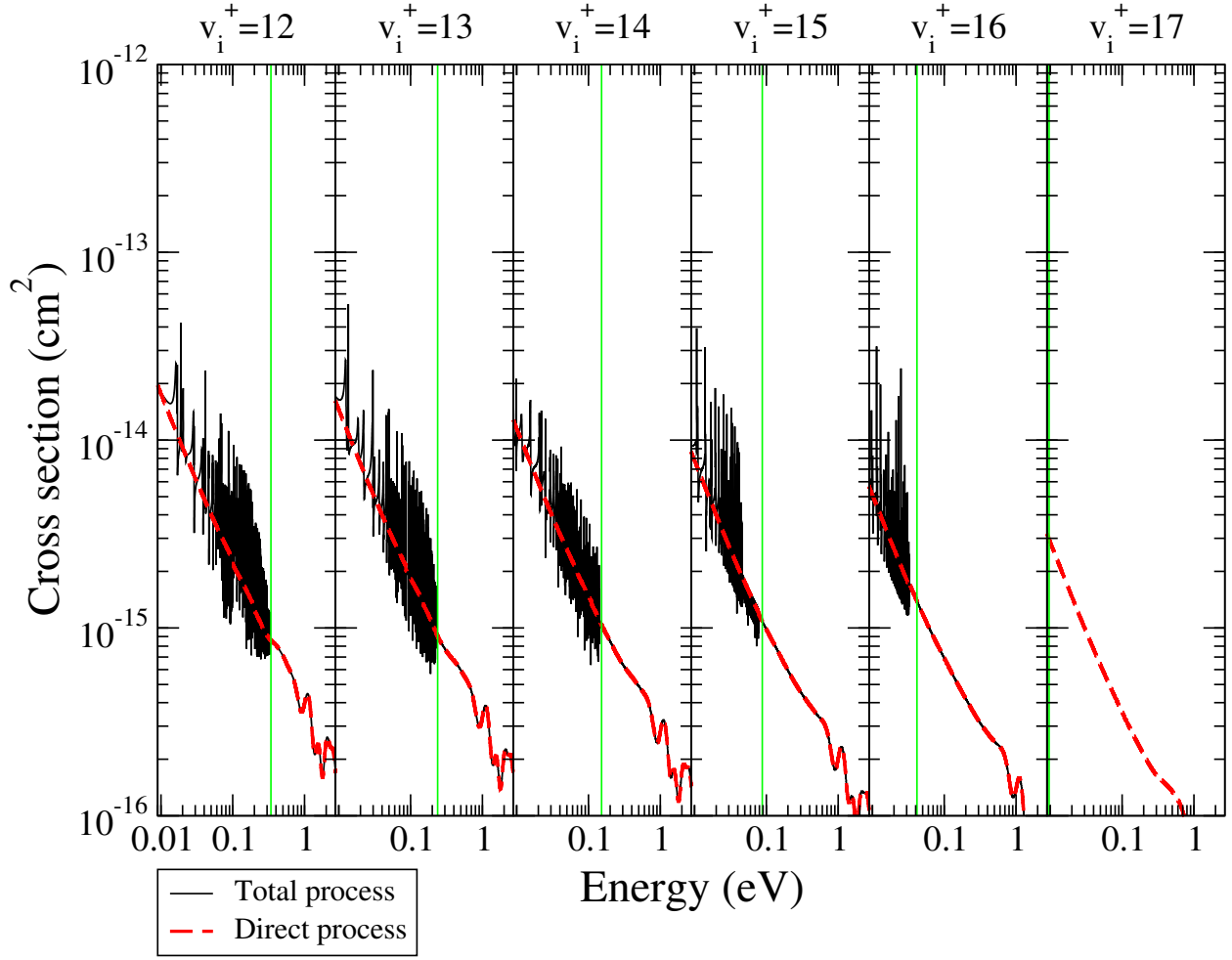
Ordinate	Maxwell rate coefficient in $\text{cm}^3 \cdot \text{s}^{-1}$
Abscissa	Electron temperature in K



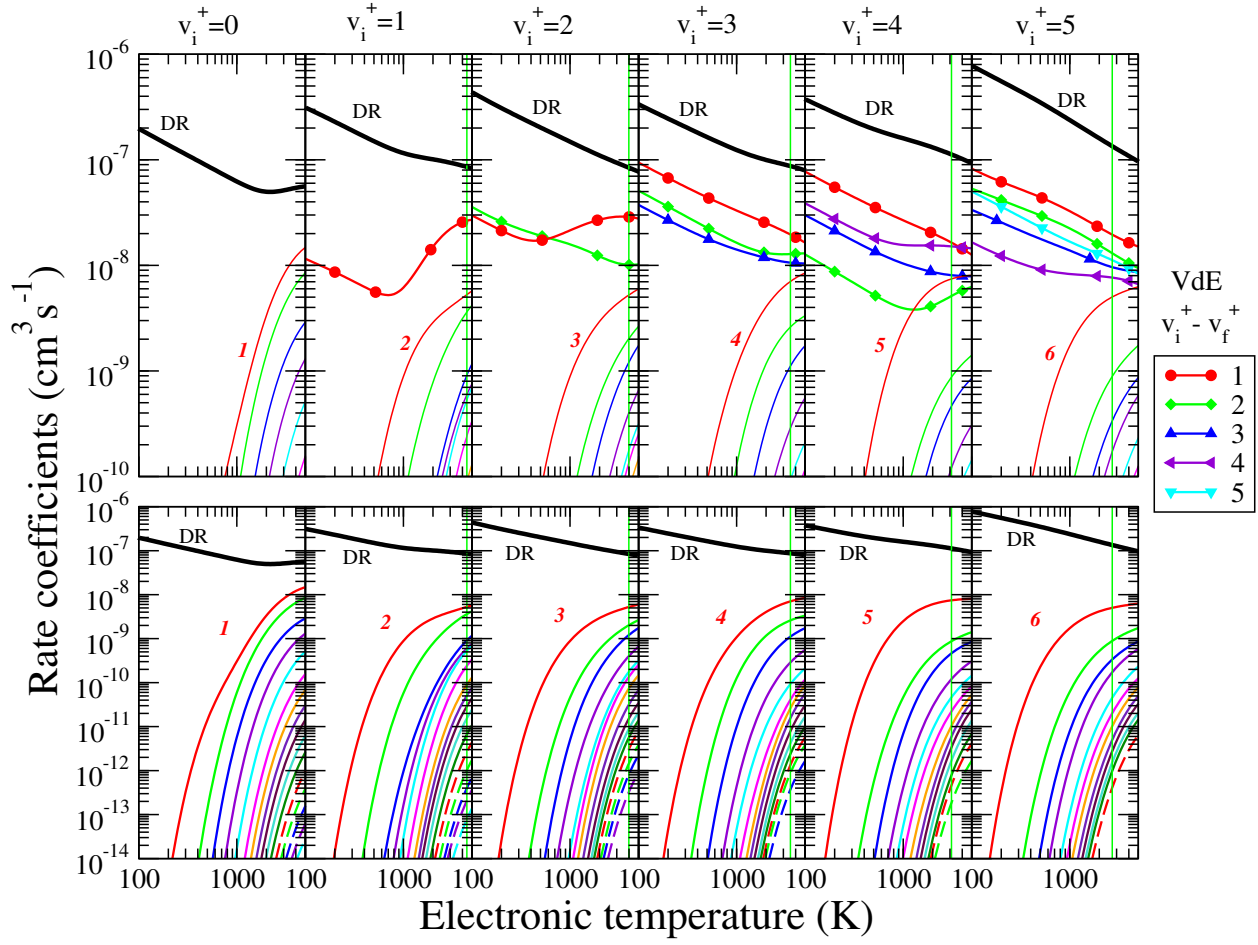
Graph 1. Dissociative recombination cross sections of ground ($v_i^+ = 0$) and excited ($v_i^+ = 1, \dots, 5$) BeH⁺ in its electronic ground state. Direct mechanism: dashed thick line, total (direct and indirect) mechanism: continuous thin line.



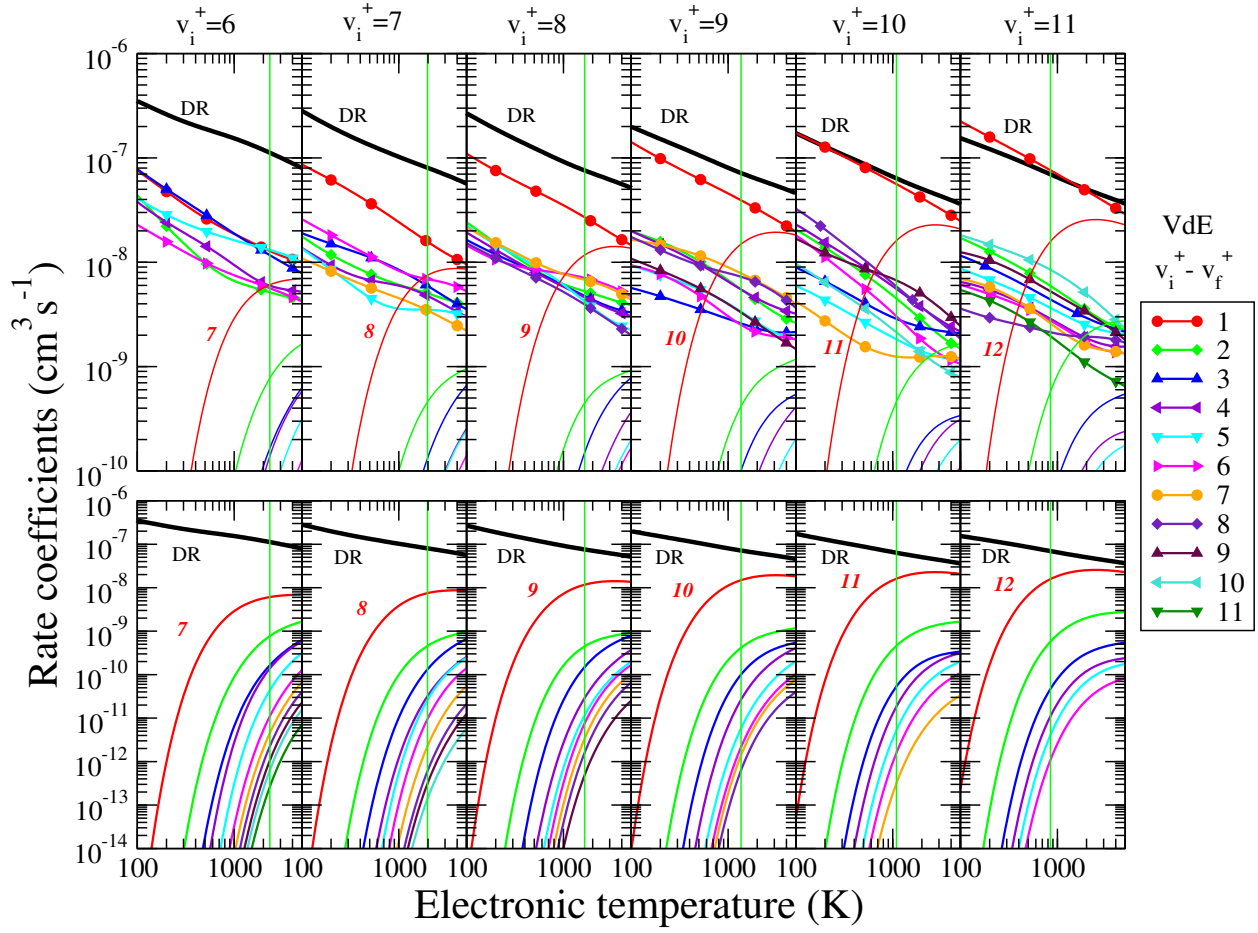
Graph 2. Dissociative recombination cross sections of excited ($v_i^+ = 6, 7, \dots, 11$) BeH^+ in its electronic ground state. Direct mechanism: dashed thick line, total (direct and indirect) mechanism: continuous thin line.



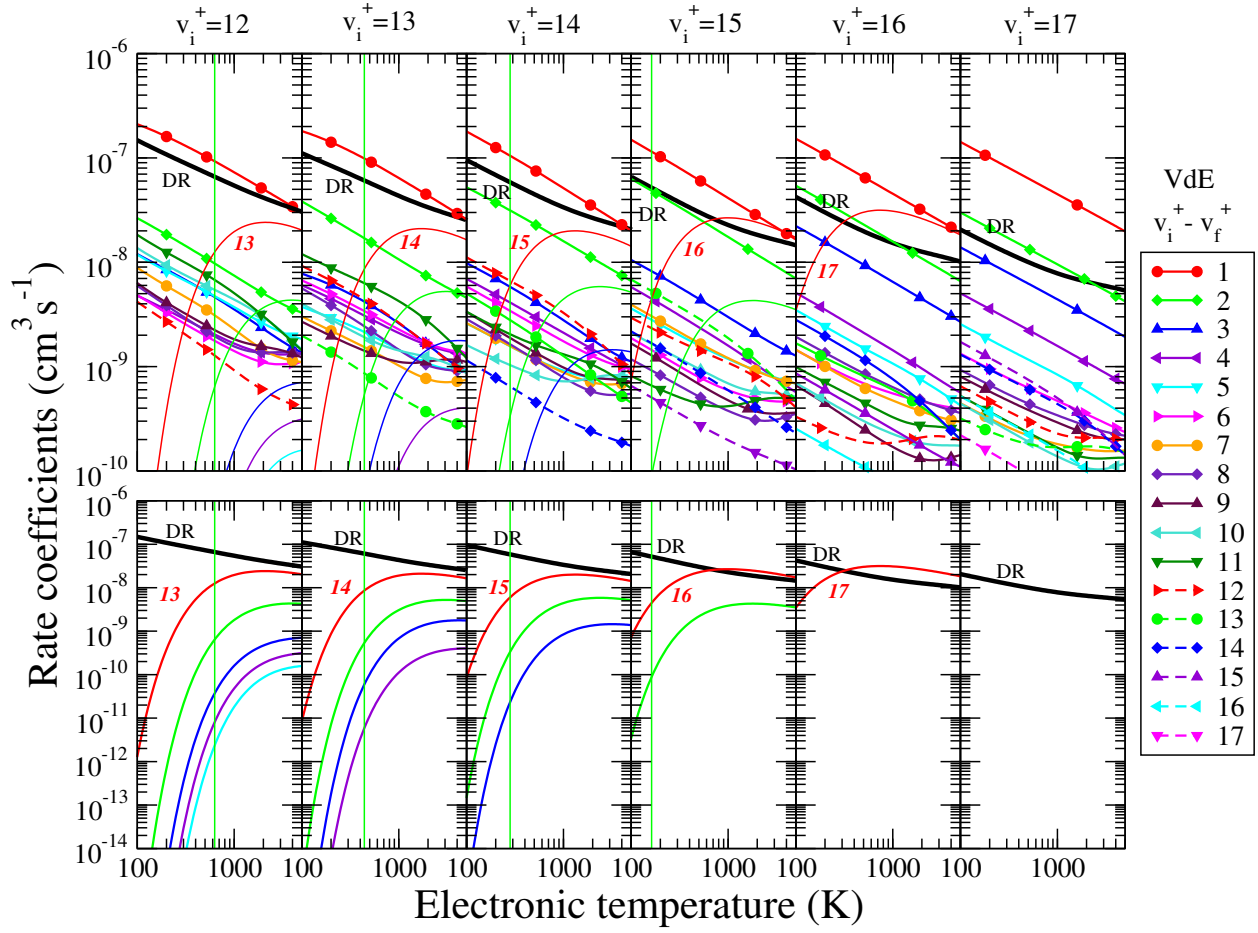
Graph 3. Dissociative recombination cross sections of excited ($v_i^+ = 12, 13, \dots, 17$) BeH^+ in its electronic ground state. Direct mechanism: dashed thick line, total (direct and indirect) mechanism: continuous thin line.



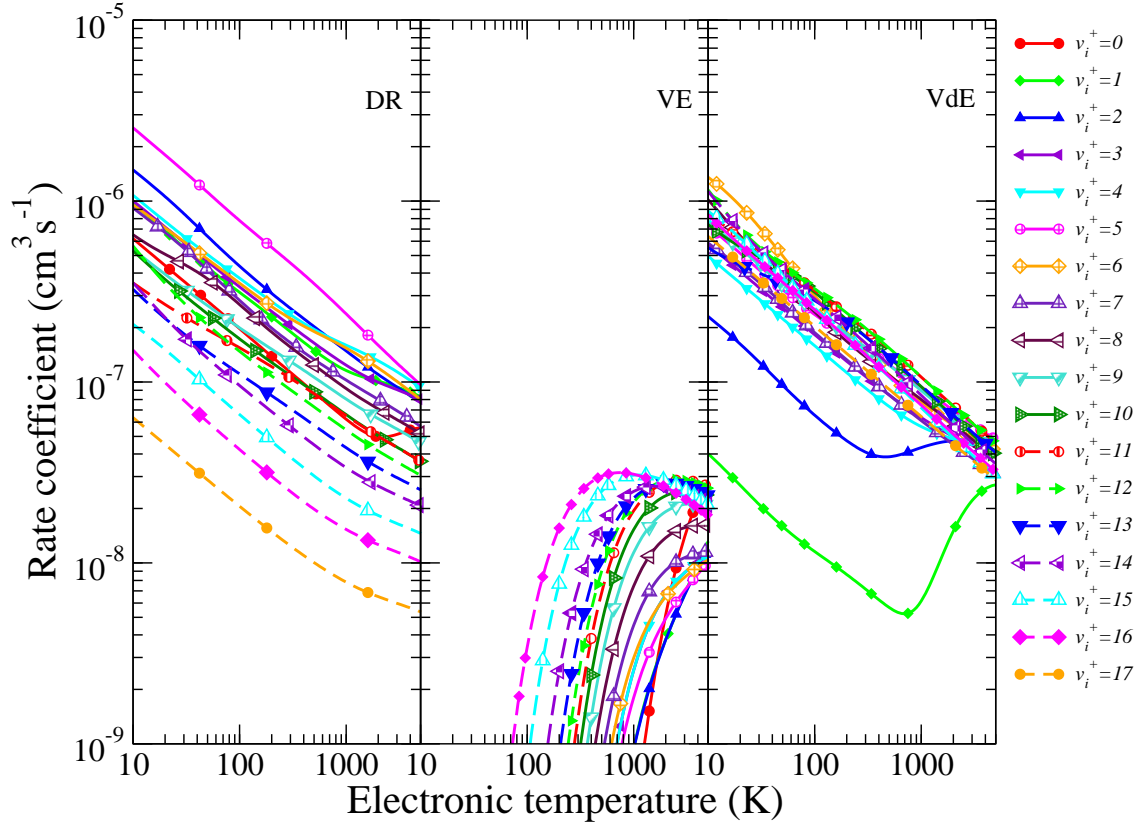
Graph 4. Dissociative recombination (DR, thick line), vibrational excitation (VE, thin lines) and vibrational de-excitation (VdE, symbols and thick lines) Maxwell rate coefficients of ground ($v_i^+ = 0$) and excited ($v_i^+ = 1, \dots, 5$) BeH⁺ in its electronic ground state (total mechanism). For VE, since the rate coefficients decrease monotonically with the excitation, the lowest final vibrational quantum number of the target is indicated only, and the lower panels extend the range down to 10⁻¹⁴ cm³/s.



Graph 5. Dissociative recombination (DR, thick line), vibrational excitation (VE, thin lines) and vibrational de-excitation (VdE, symbols and thick lines) Maxwell rate coefficients of excited ($v_i^+ = 7, 8, \dots, 11$) BeH⁺ in its electronic ground state (total mechanism). For VE, since the rate coefficients decrease monotonically with the excitation, the lowest final vibrational quantum number of the target is indicated only, and the lower panels extend the range down to 10^{-14} cm³/s.



Graph 6. Dissociative recombination (DR, thick line), vibrational excitation (VE, thin lines) and vibrational de-excitation (VdE, symbols and thick lines) Maxwell rate coefficients of excited ($v_i^+ = 12, 13, \dots, 17$) BeH^+ in its electronic ground state (total mechanism). For VE, since the rate coefficients decrease monotonically with the excitation, the lowest final vibrational quantum number of the target is indicated only, and the lower panels extend the range down to 10^{-14} cm^3/s .



Graph 7. Global (sum over all the possible final states) Maxwell rate coefficients for dissociative recombination (DR), vibrational excitation (VE) and vibrational de-excitation (VdE).

Explanation of Tables

Table 1 List of fitting parameters according to eq. (10) with 'P'='DR' and 'L'= v_i^+ ' calculated for dissociative recombination for all vibrational levels of the ground electronic state of BeH^+ .

v_i^+	Initial vibrational level of BeH^+
$A_{v_i^+}, \alpha_{v_i^+}, B_{v_i^+}(j = 1, \dots, 7)$	Fitting parameters

Tables 2-10 List of fitting parameters according to eq. (10) with 'P'='VE' or 'VdE' and 'L'= $v_i^+ \rightarrow v_f^+$ ' calculated for vibrational transitions (excitation and de-excitation) between the vibrational levels of the ground electronic state of BeH^+ .

$v_i^+ \rightarrow v_f^+$	Vibrational transition of BeH^+
$v_i^+ \rightarrow v_f^+$	Stands for VdE
$A_{v_i^+ \rightarrow v_f^+}, \alpha_{v_i^+ \rightarrow v_f^+}, B_{v_i^+ \rightarrow v_f^+}(j = 1, \dots, 7)$	Fitting parameters

Table 1 List of the parameters used in Eq.(10) for the DR Maxwell rate coefficients of BeH⁺ ($v_i^+ = 0, 1, 2, 3, \dots, 17$) displayed in Graphs 4, 5, and 6.

v_i^+	$A_{v_i^+}$	$\alpha_{v_i^+}$	$B_{v_i^+}(1)$	$B_{v_i^+}(2)$	$B_{v_i^+}(3)$	$B_{v_i^+}(4)$	$B_{v_i^+}(5)$	$B_{v_i^+}(6)$	$B_{v_i^+}(7)$
0	0.253513120 × 10 ⁻⁹	0.592469479	-0.190649410 × 10 ⁴	0.123315004 × 10 ⁷	-0.388342503 × 10 ⁹	0.647265585 × 10 ¹¹	-0.566722264 × 10 ¹³	0.232068987 × 10 ¹⁵	-0.295078806 × 10 ¹⁶
1	0.314462330 × 10 ⁻⁵	-0.407538250	0.958577714 × 10 ³	-0.135957934 × 10 ⁷	0.725436198 × 10 ⁹	-0.192640935 × 10 ¹²	0.271812541 × 10 ¹⁴	-0.194705942 × 10 ¹⁶	0.557221814 × 10 ¹⁷
2	0.114678715 × 10 ⁻⁵	-0.322376187	-0.265630394 × 10 ³	0.219601686 × 10 ⁶	-0.916549130 × 10 ⁸	0.207255861 × 10 ¹¹	-0.259613563 × 10 ¹³	0.169396374 × 10 ¹⁵	-0.449074035 × 10 ¹⁶
3	0.849641548 × 10 ⁻⁶	-0.275140774	0.171673351 × 10 ³	-0.451956583 × 10 ⁶	0.285090525 × 10 ⁹	-0.827403486 × 10 ¹¹	0.123588751 × 10 ¹⁴	-0.921680323 × 10 ¹⁵	0.271612346 × 10 ¹⁷
4	0.121239628 × 10 ⁻⁴	-0.555845997 × 10 ⁰⁰	0.761294556 × 10 ⁰³	-0.714351056 × 10 ⁰⁶	0.302073187 × 10 ⁰⁹	-0.687621706 × 10 ¹¹	0.869454121 × 10 ¹³	-0.574150868 × 10 ¹⁵	0.154263413 × 10 ¹⁷
5	0.644139392 × 10 ⁻⁰⁵	-0.498481741 × 10 ⁰⁰	-0.238774152 × 10 ⁰³	0.250065677 × 10 ⁰⁶	-0.107836783 × 10 ⁰⁹	0.245547321 × 10 ¹¹	-0.309392723 × 10 ¹³	0.203550809 × 10 ¹⁵	-0.545188444 × 10 ¹⁶
6	0.792927406 × 10 ⁻⁰⁵	-0.532262180 × 10 ⁰⁰	0.333511522 × 10 ⁰³	-0.148501292 × 10 ⁰⁶	0.171708872 × 10 ⁰⁸	-0.305133187 × 10 ¹⁰	0.998389272 × 10 ¹²	0.951736825 × 10 ¹⁴	-0.314431818 × 10 ¹⁶
7	0.316082893 × 10 ⁻⁰⁵	-0.464044213 × 10 ⁰⁰	0.378727499 × 10 ⁰³	-0.429350551 × 10 ⁰⁶	0.209573437 × 10 ⁰⁹	-0.539720017 × 10 ¹¹	0.755406940 × 10 ¹³	-0.541653151 × 10 ¹⁵	0.155580261 × 10 ¹⁷
8	0.127720970 × 10 ⁻⁰⁵	-0.373686201 × 10 ⁰⁰	0.152441331 × 10 ⁰³	-0.316359736 × 10 ⁰⁶	0.194189734 × 10 ⁰⁹	-0.564294385 × 10 ¹¹	0.847345970 × 10 ¹³	-0.634811006 × 10 ¹⁵	0.187696144 × 10 ¹⁷
9	0.746563851 × 10 ⁻⁰⁶	-0.324031010 × 10 ⁰⁰	0.602818545 × 10 ⁰²	-0.264262880 × 10 ⁰⁶	0.182715389 × 10 ⁰⁹	-0.556978341 × 10 ¹¹	0.856967656 × 10 ¹³	-0.651236746 × 10 ¹⁵	0.194333293 × 10 ¹⁷
10	0.948137849 × 10 ⁻⁰⁶	-0.381796840 × 10 ⁰⁰	0.931384032 × 10 ⁰²	-0.208870046 × 10 ⁰⁶	0.137643531 × 10 ⁰⁹	-0.416615842 × 10 ¹¹	0.641435330 × 10 ¹³	-0.488698384 × 10 ¹⁵	0.146250207 × 10 ¹⁷
11	0.563130612 × 10 ⁻⁰⁶	-0.323115264 × 10 ⁰⁰	-0.776072519 × 10 ⁰²	-0.174245951 × 10 ⁰⁵	0.408441685 × 10 ⁰⁸	-0.157643238 × 10 ¹¹	0.268014834 × 10 ¹³	-0.214967882 × 10 ¹⁵	0.663202358 × 10 ¹⁶
12	0.357088588 × 10 ⁻⁰⁶	-0.292809009 × 10 ⁰⁰	-0.171384790 × 10 ⁰³	0.637053725 × 10 ⁰⁵	0.331302643 × 10 ⁰⁶	-0.522256641 × 10 ¹⁰	0.120880459 × 10 ¹³	-0.110338393 × 10 ¹⁵	0.365644426 × 10 ¹⁶
13	0.238146575 × 10 ⁻⁰⁶	-0.266531461 × 10 ⁰⁰	-0.149024270 × 10 ⁰³	0.450300500 × 10 ⁰⁴	0.372465125 × 10 ⁰⁸	-0.154556208 × 10 ¹¹	0.268968000 × 10 ¹³	-0.215092036 × 10 ¹⁵	0.664744576 × 10 ¹⁶
14	0.168221482 × 10 ⁻⁰⁶	-0.248346800 × 10 ⁰⁰	-0.686636153 × 10 ⁰²	-0.133880711 × 10 ⁰⁶	0.108346291 × 10 ⁰⁹	-0.336011608 × 10 ¹¹	0.515157377 × 10 ¹³	-0.388887599 × 10 ¹⁵	0.115322733 × 10 ¹⁷
15	0.963114751 × 10 ⁻⁰⁷	-0.223238067 × 10 ⁰⁰	-0.444679442 × 10 ⁰²	-0.183672027 × 10 ⁰⁶	0.131718356 × 10 ⁰⁹	-0.388717436 × 10 ¹¹	0.579182824 × 10 ¹³	-0.429232314 × 10 ¹⁵	0.125677651 × 10 ¹⁷
16	0.102230026 × 10 ⁻⁰⁶	-0.267758971 × 10 ⁰⁰	0.185492363 × 10 ⁰³	-0.402541319 × 10 ⁰⁶	0.230431741 × 10 ⁰⁹	-0.630920454 × 10 ¹¹	0.907572842 × 10 ¹³	-0.659557618 × 10 ¹⁵	0.190779767 × 10 ¹⁷
17	0.342524475 × 10 ⁻⁰⁷	-0.216559518 × 10 ⁰⁰	0.797228910 × 10 ⁰²	-0.306916646 × 10 ⁰⁶	0.191881080 × 10 ⁰⁹	-0.547379843 × 10 ¹¹	0.806335965 × 10 ¹³	-0.594963683 × 10 ¹⁵	0.173892153 × 10 ¹⁷

Table 2 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH⁺ ($v_i^+ = 0$ and 1) represented in the upper panels of Graph 4.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
0 \rightarrow 1	0.124244699 $\times 10^{-01}$	-0.133548647 $\times 10^{+01}$	0.125068733 $\times 10^{+05}$	-0.119462867 $\times 10^{+08}$	0.612265338 $\times 10^{+10}$	-0.159115695 $\times 10^{+13}$	0.221261867 $\times 10^{+15}$	-0.156815975 $\times 10^{+17}$	0.444766919 $\times 10^{+18}$
0 \rightarrow 2	0.129961950 $\times 10^{-04}$	-0.661035442 $\times 10^{+00}$	0.875512695 $\times 10^{+04}$	-0.266357941 $\times 10^{+07}$	0.108710933 $\times 10^{+10}$	-0.242430358 $\times 10^{+12}$	0.306483606 $\times 10^{+14}$	-0.205871435 $\times 10^{+16}$	0.569537410 $\times 10^{+17}$
0 \rightarrow 3	0.142379982 $\times 10^{-04}$	-0.764830977 $\times 10^{+00}$	0.101101728 $\times 10^{+05}$	-0.205253723 $\times 10^{+07}$	0.137208247 $\times 10^{+10}$	-0.493436150 $\times 10^{+12}$	0.974091099 $\times 10^{+14}$	-0.991580495 $\times 10^{+16}$	0.405560372 $\times 10^{+17}$
0 \rightarrow 4	0.613107973 $\times 10^{-05}$	-0.715948096 $\times 10^{+00}$	0.116459658 $\times 10^{+05}$	0.180037625 $\times 10^{+07}$	-0.380655693 $\times 10^{+10}$	0.289048070 $\times 10^{+13}$	-0.104565345 $\times 10^{+16}$	0.181732642 $\times 10^{+18}$	-0.121943739 $\times 10^{+20}$
0 \rightarrow 5	0.454423919 $\times 10^{-05}$	-0.724833034 $\times 10^{+00}$	0.144167691 $\times 10^{+05}$	0.187042671 $\times 10^{+07}$	-0.553846921 $\times 10^{+10}$	0.525679261 $\times 10^{+13}$	-0.238384685 $\times 10^{+16}$	0.498406730 $\times 10^{+18}$	-0.410070468 $\times 10^{+20}$
0 \rightarrow 6	0.779183743 $\times 10^{-05}$	-0.847008699 $\times 10^{+00}$	0.181829327 $\times 10^{+05}$	-0.181366766 $\times 10^{+07}$	-0.132640151 $\times 10^{+10}$	0.318338532 $\times 10^{+13}$	-0.206370313 $\times 10^{+16}$	0.581977441 $\times 10^{+18}$	-0.613361897 $\times 10^{+20}$
0 \rightarrow 7	0.180900968 $\times 10^{-05}$	-0.769516882 $\times 10^{+00}$	0.174642032 $\times 10^{+05}$	0.933492644 $\times 10^{+07}$	-0.212163824 $\times 10^{+11}$	0.224415719 $\times 10^{+14}$	-0.123418778 $\times 10^{+17}$	0.339594431 $\times 10^{+19}$	-0.369092511 $\times 10^{+21}$
0 \rightarrow 8	0.885677466 $\times 10^{-06}$	-0.75779635 $\times 10^{+00}$	0.179047867 $\times 10^{+05}$	0.166541738 $\times 10^{+08}$	-0.37830799 $\times 10^{+11}$	0.425126855 $\times 10^{+14}$	-0.252095351 $\times 10^{+17}$	0.753876184 $\times 10^{+19}$	-0.894639753 $\times 10^{+21}$
0 \rightarrow 9	0.292847848 $\times 10^{-05}$	-0.931863593 $\times 10^{+00}$	0.202925021 $\times 10^{+05}$	0.165263943 $\times 10^{+08}$	-0.417425440 $\times 10^{+11}$	0.513399746 $\times 10^{+15}$	-0.332126562 $\times 10^{+17}$	0.108344862 $\times 10^{+20}$	-0.140382835 $\times 10^{+22}$
0 \rightarrow 10	0.375829669 $\times 10^{-17}$	0.172904099 $\times 10^{+01}$	-0.949241046 $\times 10^{+04}$	0.152679710 $\times 10^{+09}$	-0.333798077 $\times 10^{+12}$	0.390903195 $\times 10^{+15}$	-0.250274637 $\times 10^{+18}$	0.823914165 $\times 10^{+20}$	-0.108923336 $\times 10^{+23}$
0 \rightarrow 11	0.261968821 $\times 10^{-13}$	0.774835837 $\times 10^{+00}$	0.117881450 $\times 10^{+04}$	0.118759130 $\times 10^{+09}$	-0.275480710 $\times 10^{+12}$	0.34345630 $\times 10^{+15}$	-0.235068413 $\times 10^{+18}$	0.8300049285 $\times 10^{+20}$	-0.117994706 $\times 10^{+23}$
0 \rightarrow 12	0.881455067 $\times 10^{-10}$	-0.113146035 $\times 10^{+00}$	0.119234535 $\times 10^{+05}$	0.792457916 $\times 10^{+08}$	-0.194518373 $\times 10^{+12}$	0.257071238 $\times 10^{+15}$	-0.187454839 $\times 10^{+18}$	0.708187002 $\times 10^{+20}$	-0.108036847 $\times 10^{+23}$
0 \rightarrow 13	0.144309667 $\times 10^{-20}$	0.225970970 $\times 10^{+01}$	-0.174823864 $\times 10^{+05}$	0.228436065 $\times 10^{+09}$	-0.564780467 $\times 10^{+12}$	0.765207700 $\times 10^{+15}$	-0.575653243 $\times 10^{+18}$	0.224947435 $\times 10^{+21}$	-0.355386076 $\times 10^{+23}$
0 \rightarrow 14	0.515928934 $\times 10^{-33}$	0.500054420 $\times 10^{+01}$	-0.527361648 $\times 10^{+05}$	0.412102666 $\times 10^{+09}$	-0.104124985 $\times 10^{+13}$	0.144983244 $\times 10^{+16}$	-0.112378255 $\times 10^{+19}$	0.453177248 $\times 10^{+21}$	-0.739667532 $\times 10^{+23}$
0 \rightarrow 15	0.409733697 $\times 10^{-30}$	0.424682138 $\times 10^{+01}$	-0.444964251 $\times 10^{+05}$	0.384057361 $\times 10^{+09}$	-0.100210836 $\times 10^{+13}$	0.144676938 $\times 10^{+16}$	-0.116586218 $\times 10^{+19}$	0.489738407 $\times 10^{+21}$	-0.833887502 $\times 10^{+23}$
0 \rightarrow 16	0.817690729 $\times 10^{-15}$	0.703951856 $\times 10^{+00}$	0.112434814 $\times 10^{+04}$	0.157806613 $\times 10^{+09}$	-0.429889131 $\times 10^{+12}$	0.650940867 $\times 10^{+15}$	-0.552117504 $\times 10^{+18}$	0.244767149 $\times 10^{+21}$	-0.440734326 $\times 10^{+23}$
0 \rightarrow 17	0.318362667 $\times 10^{-07}$	-0.112905511 $\times 10^{+01}$	0.258463367 $\times 10^{+05}$	0.286089905 $\times 10^{+08}$	-0.817025631 $\times 10^{+11}$	0.130297321 $\times 10^{+15}$	-0.116894583 $\times 10^{+18}$	0.549998801 $\times 10^{+20}$	-0.105390504 $\times 10^{+23}$
1 \rightarrow 0	0.119995521 $\times 10^{-01}$	-0.133145724 $\times 10^{+01}$	0.949370743 $\times 10^{+04}$	-0.119324786 $\times 10^{+08}$	0.611542737 $\times 10^{+10}$	-0.158919832 $\times 10^{+13}$	0.220977965 $\times 10^{+15}$	-0.156607293 $\times 10^{+17}$	0.444156376 $\times 10^{+18}$
1 \rightarrow 2	0.153405809 $\times 10^{-09}$	0.434544617 $\times 10^{+00}$	0.126900527 $\times 10^{+03}$	0.316420456 $\times 10^{+07}$	-0.162425671 $\times 10^{+10}$	0.428949781 $\times 10^{+12}$	-0.607065893 $\times 10^{+14}$	0.437214022 $\times 10^{+16}$	-0.125745509 $\times 10^{+18}$
1 \rightarrow 3	0.43891959 $\times 10^{-09}$	0.363985856 $\times 10^{+00}$	0.410517739 $\times 10^{+04}$	0.114700075 $\times 10^{+07}$	-0.465492198 $\times 10^{+09}$	0.111603719 $\times 10^{+12}$	-0.156948862 $\times 10^{+14}$	0.118915651 $\times 10^{+16}$	-0.372436135 $\times 10^{+17}$
1 \rightarrow 4	0.236206473 $\times 10^{-08}$	0.152020035 $\times 10^{+00}$	0.104026260 $\times 10^{+05}$	-0.487621366 $\times 10^{+07}$	0.343240714 $\times 10^{+10}$	-0.110471209 $\times 10^{+13}$	0.171900079 $\times 10^{+15}$	-0.114545501 $\times 10^{+17}$	0.179064658 $\times 10^{+18}$
1 \rightarrow 5	0.152191494 $\times 10^{-09}$	0.345225244 $\times 10^{+00}$	0.513753422 $\times 10^{+04}$	0.178355178 $\times 10^{+08}$	-0.225274397 $\times 10^{+11}$	0.138279944 $\times 10^{+14}$	-0.439165696 $\times 10^{+16}$	0.693264288 $\times 10^{+18}$	-0.429807741 $\times 10^{+20}$
1 \rightarrow 6	0.101510366 $\times 10^{-10}$	0.631699375 $\times 10^{+00}$	0.288258591 $\times 10^{+04}$	0.345014862 $\times 10^{+08}$	-0.493043937 $\times 10^{+11}$	0.351403621 $\times 10^{+14}$	-0.131109063 $\times 10^{+17}$	0.244599334 $\times 10^{+19}$	-0.179832560 $\times 10^{+21}$
1 \rightarrow 7	0.503759081 $\times 10^{-14}$	0.136346953 $\times 10^{+01}$	-0.282054702 $\times 10^{+04}$	0.655513089 $\times 10^{+08}$	-0.104669273 $\times 10^{+12}$	0.846366689 $\times 10^{+14}$	-0.361353660 $\times 10^{+17}$	0.775870551 $\times 10^{+19}$	-0.059112966 $\times 10^{+21}$
1 \rightarrow 8	0.104460699 $\times 10^{-22}$	0.329471379 $\times 10^{+01}$	-0.222066050 $\times 10^{+05}$	0.146482864 $\times 10^{+09}$	-0.248918167 $\times 10^{+12}$	0.219701804 $\times 10^{+15}$	-0.103979287 $\times 10^{+18}$	0.249845144 $\times 10^{+20}$	-0.238977274 $\times 10^{+22}$
1 \rightarrow 9	0.770482688 $\times 10^{-19}$	0.233273067 $\times 10^{+01}$	-0.149429814 $\times 10^{+05}$	0.136734073 $\times 10^{+09}$	-0.251527270 $\times 10^{+12}$	0.242731069 $\times 10^{+15}$	-0.126489623 $\times 10^{+18}$	0.336140544 $\times 10^{+20}$	-0.356623146 $\times 10^{+22}$
1 \rightarrow 10	0.438603837 $\times 10^{-43}$	0.788846091 $\times 10^{+01}$	-0.730962596 $\times 10^{+05}$	0.371153627 $\times 10^{+09}$	-0.701373815 $\times 10^{+12}$	0.704940585 $\times 10^{+15}$	-0.384794261 $\times 10^{+18}$	0.107432846 $\times 10^{+21}$	-0.119977129 $\times 10^{+23}$
1 \rightarrow 11	0.320761937 $\times 10^{-24}$	0.347485090 $\times 10^{+01}$	-0.283733940 $\times 10^{+05}$	0.215297915 $\times 10^{+09}$	-0.436678198 $\times 10^{+12}$	0.473346729 $\times 10^{+15}$	-0.279759433 $\times 10^{+18}$	0.848241442 $\times 10^{+20}$	-0.103105452 $\times 10^{+23}$
1 \rightarrow 12	0.113204823 $\times 10^{-03}$	-0.131225290 $\times 10^{+01}$	0.246991254 $\times 10^{+05}$	0.431579951 $\times 10^{+07}$	-0.157723943 $\times 10^{+11}$	0.223768013 $\times 10^{+14}$	-0.159834373 $\times 10^{+17}$	0.568566052 $\times 10^{+19}$	-0.800164550 $\times 10^{+21}$
1 \rightarrow 13	0.104988047 $\times 10^{-74}$	0.148966581 $\times 10^{+02}$	-0.159227178 $\times 10^{+06}$	0.808002769 $\times 10^{+09}$	-0.174489353 $\times 10^{+13}$	0.203780599 $\times 10^{+16}$	-0.130694229 $\times 10^{+19}$	0.432028955 $\times 10^{+21}$	-0.574347050 $\times 10^{+23}$
1 \rightarrow 14	0.180099766 $\times 10^{-89}$	0.181631747 $\times 10^{+02}$	-0.201181188 $\times 10^{+06}$	0.102436792 $\times 10^{+10}$	-0.228735959 $\times 10^{+13}$	0.277407933 $\times 10^{+16}$	-0.185325477 $\times 10^{+19}$	0.639479025 $\times 10^{+21}$	-0.888701509 $\times 10^{+23}$
1 \rightarrow 15	0.888540666 $\times 10^{-98}$	0.199435296 $\times 10^{+02}$	-0.226741706 $\times 10^{+06}$	0.117101483 $\times 10^{+10}$	-0.269183299 $\times 10^{+13}$	0.337382650 $\times 10^{+16}$	-0.233573986 $\times 10^{+19}$	0.836822518 $\times 10^{+21}$	-0.120912586 $\times 10^{+24}$
1 \rightarrow 16	0.328338427 $\times 10^{-101}$	0.206397435 $\times 10^{+02}$	-0.238922323 $\times 10^{+06}$	0.125253606 $\times 10^{+10}$	-0.294342481 $\times 10^{+13}$	0.378225945 $\times 10^{+16}$	-0.268992435 $\times 10^{+19}$	0.991346617 $\times 10^{+21}$	-0.147482671 $\times 10^{+24}$
1 \rightarrow 17	0.174113501 $\times 10^{-52}$	0.940244289 $\times 10^{+01}$	-0.108030577 $\times 10^{+06}$	0.673355963 $\times 10^{+09}$	-0.167173275 $\times 10^{+13}$	0.227801968 $\times 10^{+16}$	-0.172196403 $\times 10^{+19}$	0.675100081 $\times 10^{+21}$	-0.106830896 $\times 10^{+24}$

Table 3 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH⁺ ($v_i^+ = 2$ and 3) represented in the upper panels of Graph 4.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
2 \rightarrow 0	0.126308415 $\times 10^{-09}$	0.456305622 $\times 10^{+00}$	-0.282698010 $\times 10^{+04}$	0.324128858 $\times 10^{+07}$	-0.166236562 $\times 10^{+10}$	0.438820087 $\times 10^{+12}$	-0.620881147 $\times 10^{+14}$	0.447096361 $\times 10^{+16}$	-0.128575131 $\times 10^{+18}$
2 \rightarrow 1	0.108956019 $\times 10^{-04}$	-0.641702757 $\times 10^{+00}$	0.276723409 $\times 10^{+04}$	-0.249602163 $\times 10^{+07}$	0.977115209 $\times 10^{+09}$	-0.206805990 $\times 10^{+12}$	0.246613751 $\times 10^{+14}$	-0.155686663 $\times 10^{+16}$	0.404532125 $\times 10^{+17}$
2 \rightarrow 3	0.296926175 $\times 10^{-08}$	0.124816242 $\times 10^{+00}$	0.173836549 $\times 10^{+04}$	0.908486506 $\times 10^{+06}$	-0.424294717 $\times 10^{+09}$	0.108080533 $\times 10^{+12}$	-0.150790846 $\times 10^{+14}$	0.107908466 $\times 10^{+16}$	-0.309653342 $\times 10^{+17}$
2 \rightarrow 4	0.233152145 $\times 10^{-08}$	0.122367759 $\times 10^{+00}$	0.452862967 $\times 10^{+04}$	0.653277887 $\times 10^{+06}$	-0.273049775 $\times 10^{+09}$	0.670734633 $\times 10^{+11}$	-0.944014877 $\times 10^{+13}$	0.700856130 $\times 10^{+15}$	-0.211863471 $\times 10^{+17}$
2 \rightarrow 5	0.179746490 $\times 10^{-09}$	0.385415212 $\times 10^{+00}$	0.455113975 $\times 10^{+04}$	0.557366075 $\times 10^{+07}$	-0.437760675 $\times 10^{+10}$	0.181187931 $\times 10^{+13}$	-0.403454650 $\times 10^{+15}$	0.458962441 $\times 10^{+17}$	-0.207392120 $\times 10^{+19}$
2 \rightarrow 6	0.662229481 $\times 10^{-13}$	0.115712028 $\times 10^{+01}$	0.161972309 $\times 10^{+04}$	0.182461133 $\times 10^{+08}$	-0.191412396 $\times 10^{+11}$	0.106134357 $\times 10^{+14}$	-0.314224909 $\times 10^{+16}$	0.468199997 $\times 10^{+18}$	-0.275398722 $\times 10^{+20}$
2 \rightarrow 7	0.145068779 $\times 10^{-16}$	0.194335259 $\times 10^{+01}$	-0.679220386 $\times 10^{+04}$	0.602954203 $\times 10^{+08}$	-0.819656147 $\times 10^{+11}$	0.556924052 $\times 10^{+14}$	-0.198435182 $\times 10^{+17}$	0.354151824 $\times 10^{+19}$	-0.249461077 $\times 10^{+21}$
2 \rightarrow 8	0.409080689 $\times 10^{-28}$	0.462578650 $\times 10^{+01}$	-0.314098439 $\times 10^{+05}$	0.145520499 $\times 10^{+09}$	-0.209844542 $\times 10^{+12}$	0.156055016 $\times 10^{+15}$	-0.618820134 $\times 10^{+17}$	0.124075458 $\times 10^{+20}$	-0.987496244 $\times 10^{+21}$
2 \rightarrow 9	0.124226786 $\times 10^{-18}$	0.235220787 $\times 10^{+01}$	-0.124786214 $\times 10^{+05}$	0.101019453 $\times 10^{+09}$	-0.163557194 $\times 10^{+12}$	0.137833270 $\times 10^{+15}$	-0.622423124 $\times 10^{+17}$	0.142528576 $\times 10^{+20}$	-0.129773407 $\times 10^{+22}$
2 \rightarrow 10	0.245518460 $\times 10^{-28}$	0.454190007 $\times 10^{+01}$	-0.339017796 $\times 10^{+05}$	0.187717660 $\times 10^{+09}$	-0.332108029 $\times 10^{+12}$	0.288460789 $\times 10^{+15}$	-0.139570052 $\times 10^{+18}$	0.343550312 $\times 10^{+20}$	-0.337037720 $\times 10^{+22}$
2 \rightarrow 11	0.587221095 $\times 10^{-38}$	0.668854662 $\times 10^{+01}$	-0.585692446 $\times 10^{+05}$	0.300404084 $\times 10^{+09}$	-0.549700752 $\times 10^{+12}$	0.532010351 $\times 10^{+15}$	-0.278620007 $\times 10^{+18}$	0.744613338 $\times 10^{+20}$	-0.794724821 $\times 10^{+22}$
2 \rightarrow 12	0.282820034 $\times 10^{-62}$	0.900692240 $\times 10^{+01}$	-0.854015521 $\times 10^{+05}$	0.421766486 $\times 10^{+09}$	-0.803276765 $\times 10^{+12}$	0.814702124 $\times 10^{+15}$	-0.449137228 $\times 10^{+18}$	0.126738498 $\times 10^{+21}$	-0.143144660 $\times 10^{+23}$
2 \rightarrow 13	0.265515367 $\times 10^{-54}$	0.103422905 $\times 10^{+02}$	-0.102161017 $\times 10^{+06}$	0.507355535 $\times 10^{+09}$	-0.100269394 $\times 10^{+13}$	0.106072719 $\times 10^{+16}$	-0.611987469 $\times 10^{+18}$	0.181152972 $\times 10^{+21}$	-0.214995200 $\times 10^{+23}$
2 \rightarrow 14	0.261195739 $\times 10^{-62}$	0.121198250 $\times 10^{+02}$	-0.123754196 $\times 10^{+06}$	0.614670324 $\times 10^{+09}$	-0.125449510 $\times 10^{+13}$	0.137621206 $\times 10^{+16}$	-0.825669890 $\times 10^{+18}$	0.254634769 $\times 10^{+21}$	-0.315273928 $\times 10^{+23}$
2 \rightarrow 15	0.337950444 $\times 10^{-70}$	0.138489790 $\times 10^{+02}$	-0.145442136 $\times 10^{+06}$	0.725912499 $\times 10^{+09}$	-0.152624068 $\times 10^{+13}$	0.173091740 $\times 10^{+16}$	-0.107614767 $\times 10^{+19}$	0.344467648 $\times 10^{+21}$	-0.443138527 $\times 10^{+23}$
2 \rightarrow 16	0.890704375 $\times 10^{-70}$	0.136862264 $\times 10^{+02}$	-0.146142169 $\times 10^{+06}$	0.748211873 $\times 10^{+09}$	-0.161520665 $\times 10^{+13}$	0.188583754 $\times 10^{+16}$	-0.120927715 $\times 10^{+19}$	0.399702625 $\times 10^{+21}$	-0.531334515 $\times 10^{+23}$
2 \rightarrow 17	0.150098120 $\times 10^{-51}$	0.940497017 $\times 10^{+01}$	-0.999890655 $\times 10^{+05}$	0.566857445 $\times 10^{+09}$	-0.126885981 $\times 10^{+13}$	0.154015811 $\times 10^{+16}$	-0.102880135 $\times 10^{+19}$	0.354673172 $\times 10^{+21}$	-0.492093817 $\times 10^{+23}$
3 \rightarrow 0	0.255293462 $\times 10^{-08}$	0.141696630 $\times 10^{+00}$	-0.108678652 $\times 10^{+04}$	0.970062410 $\times 10^{+06}$	-0.455079294 $\times 10^{+09}$	0.116124140 $\times 10^{+12}$	-0.162068475 $\times 10^{+14}$	0.116059371 $\times 10^{+16}$	-0.333086705 $\times 10^{+17}$
3 \rightarrow 1	0.454371529 $\times 10^{-09}$	0.361457499 $\times 10^{+00}$	-0.148626220 $\times 10^{+04}$	0.100937278 $\times 10^{+07}$	-0.353342852 $\times 10^{+09}$	0.694367809 $\times 10^{+11}$	-0.772450214 $\times 10^{+13}$	0.453934615 $\times 10^{+15}$	-0.109451051 $\times 10^{+17}$
3 \rightarrow 2	0.485973467 $\times 10^{-05}$	-0.651029662 $\times 10^{+00}$	0.804957988 $\times 10^{+03}$	-0.857704662 $\times 10^{+06}$	0.412563914 $\times 10^{+09}$	-0.104493488 $\times 10^{+12}$	0.143877589 $\times 10^{+14}$	-0.101687756 $\times 10^{+16}$	0.288548713 $\times 10^{+17}$
3 \rightarrow 4	0.232467658 $\times 10^{-06}$	-0.302405394 $\times 10^{+00}$	0.384019801 $\times 10^{+04}$	-0.156393045 $\times 10^{+07}$	0.782465204 $\times 10^{+09}$	-0.197911019 $\times 10^{+12}$	0.269171925 $\times 10^{+14}$	-0.187489378 $\times 10^{+16}$	0.524590130 $\times 10^{+17}$
3 \rightarrow 5	0.440932239 $\times 10^{-06}$	-0.461349565 $\times 10^{+00}$	0.470955951 $\times 10^{+04}$	0.763181298 $\times 10^{+06}$	-0.430728638 $\times 10^{+09}$	0.118093902 $\times 10^{+12}$	-0.170152283 $\times 10^{+14}$	0.123756313 $\times 10^{+16}$	-0.358125341 $\times 10^{+17}$
3 \rightarrow 6	0.248118257 $\times 10^{-07}$	-0.176014398 $\times 10^{+00}$	0.546411270 $\times 10^{+04}$	0.382709019 $\times 10^{+07}$	-0.321036040 $\times 10^{+10}$	0.136543056 $\times 10^{+13}$	-0.304649186 $\times 10^{+15}$	0.339316565 $\times 10^{+17}$	-0.148556841 $\times 10^{+19}$
3 \rightarrow 7	0.552823502 $\times 10^{-14}$	-0.853326551 $\times 10^{-01}$	0.738084609 $\times 10^{+04}$	0.509493799 $\times 10^{+07}$	-0.452686316 $\times 10^{+10}$	0.206014096 $\times 10^{+13}$	-0.507840858 $\times 10^{+15}$	0.645396348 $\times 10^{+17}$	-0.331488284 $\times 10^{+19}$
3 \rightarrow 8	0.556027551 $\times 10^{-14}$	0.128059714 $\times 10^{+01}$	-0.722375766 $\times 10^{+03}$	0.293329373 $\times 10^{+08}$	-0.332551286 $\times 10^{+11}$	0.200746468 $\times 10^{+14}$	-0.655614154 $\times 10^{+16}$	0.108966954 $\times 10^{+19}$	-0.720949572 $\times 10^{+20}$
3 \rightarrow 9	0.105702929 $\times 10^{-22}$	0.332530499 $\times 10^{+01}$	-0.159170215 $\times 10^{+05}$	0.877638068 $\times 10^{+08}$	-0.123120535 $\times 10^{+12}$	0.891243930 $\times 10^{+14}$	-0.342208461 $\times 10^{+17}$	0.661104891 $\times 10^{+19}$	-0.505031277 $\times 10^{+21}$
3 \rightarrow 10	0.873323579 $\times 10^{-29}$	0.471156180 $\times 10^{+01}$	-0.309840419 $\times 10^{+05}$	0.157565181 $\times 10^{+09}$	-0.245838938 $\times 10^{+12}$	0.197254981 $\times 10^{+15}$	-0.842530563 $\times 10^{+17}$	0.181826211 $\times 10^{+20}$	-0.155700530 $\times 10^{+22}$
3 \rightarrow 11	0.161691663 $\times 10^{-11}$	0.625264862 $\times 10^{+00}$	0.44356063 $\times 10^{+04}$	0.571317412 $\times 10^{+08}$	-0.111444978 $\times 10^{+12}$	0.108422852 $\times 10^{+15}$	-0.553083542 $\times 10^{+17}$	0.141285569 $\times 10^{+20}$	-0.142346921 $\times 10^{+22}$
3 \rightarrow 12	0.996158345 $\times 10^{-32}$	0.526593701 $\times 10^{+01}$	-0.410318341 $\times 10^{+05}$	0.225769847 $\times 10^{+09}$	-0.403565597 $\times 10^{+12}$	0.377112648 $\times 10^{+15}$	-0.189442841 $\times 10^{+18}$	0.483813236 $\times 10^{+20}$	-0.492309385 $\times 10^{+22}$
3 \rightarrow 13	0.137490891 $\times 10^{-39}$	0.701036896 $\times 10^{+01}$	-0.611600724 $\times 10^{+05}$	0.314708823 $\times 10^{+09}$	-0.582135637 $\times 10^{+12}$	0.568238103 $\times 10^{+15}$	-0.300018662 $\times 10^{+18}$	0.808463515 $\times 10^{+20}$	-0.870338374 $\times 10^{+22}$
3 \rightarrow 14	0.137970987 $\times 10^{-46}$	0.855396426 $\times 10^{+01}$	-0.797231356 $\times 10^{+05}$	0.398979415 $\times 10^{+09}$	-0.761023171 $\times 10^{+12}$	0.771557989 $\times 10^{+15}$	-0.424818758 $\times 10^{+18}$	0.119669980 $\times 10^{+21}$	-0.134890370 $\times 10^{+23}$
3 \rightarrow 15	0.188321221 $\times 10^{-48}$	0.891102185 $\times 10^{+01}$	-0.858227282 $\times 10^{+05}$	0.435553030 $\times 10^{+09}$	-0.854746186 $\times 10^{+12}$	0.895329760 $\times 10^{+15}$	-0.510613712 $\times 10^{+18}$	0.149231738 $\times 10^{+21}$	-0.174715509 $\times 10^{+23}$
3 \rightarrow 16	0.253259645 $\times 10^{-45}$	0.814294465 $\times 10^{+01}$	-0.788662325 $\times 10^{+05}$	0.416268987 $\times 10^{+09}$	-0.832962953 $\times 10^{+12}$	0.891831242 $\times 10^{+15}$	-0.520838344 $\times 10^{+18}$	0.156096398 $\times 10^{+21}$	-0.187612211 $\times 10^{+23}$
3 \rightarrow 17	0.880763483 $\times 10^{-59}$	0.111500449 $\times 10^{+02}$	-0.112805620 $\times 10^{+06}$	0.563857769 $\times 10^{+09}$	-0.114647825 $\times 10^{+13}$	0.125089015 $\times 10^{+16}$	-0.745700701 $\times 10^{+18}$	0.228371168 $\times 10^{+21}$	-0.280672906 $\times 10^{+23}$

Table 4 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH^+ ($v_i^+ = 4$ and 5) represented in the upper panels of Graph 4.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
4 \rightarrow 0	.358062377 $\times 10^{-07}$	-.111707819 $\times 10^{00}$	-.523486685 $\times 10^{03}$.372738921 $\times 10^{07}$	-.678756195 $\times 10^{10}$.539351308 $\times 10^{13}$	-.218437908 $\times 10^{16}$.443605968 $\times 10^{18}$	-.358959655 $\times 10^{20}$
4 \rightarrow 1	.604013983 $\times 10^{-09}$.265464781 $\times 10^{00}$	-.175674106 $\times 10^{04}$.244338137 $\times 10^{07}$	-.200984104 $\times 10^{10}$.931164967 $\times 10^{12}$	-.231463009 $\times 10^{15}$.271464752 $\times 10^{17}$	-.992843627 $\times 10^{18}$
4 \rightarrow 2	.623253104 $\times 10^{-03}$	-.112985446 $\times 10^{01}$.121940642 $\times 10^{05}$	-.321116064 $\times 10^{08}$.376208253 $\times 10^{11}$	-.237896655 $\times 10^{14}$.841392067 $\times 10^{16}$	-.156579408 $\times 10^{19}$	-.119370657 $\times 10^{21}$
4 \rightarrow 3	.160723340 $\times 10^{-03}$	-.104889329 $\times 10^{01}$.314477056 $\times 10^{04}$	-.619056009 $\times 10^{07}$.640948266 $\times 10^{10}$	-.381013560 $\times 10^{13}$.130237723 $\times 10^{16}$	-.237528849 $\times 10^{18}$.178829597 $\times 10^{20}$
4 \rightarrow 4	.110993265 $\times 10^{-07}$	-.359602680 $\times 10^{-01}$	-.506031232 $\times 10^{03}$.660311514 $\times 10^{07}$	-.716707150 $\times 10^{10}$.440032207 $\times 10^{13}$	-.154246121 $\times 10^{16}$.286977165 $\times 10^{18}$	-.219488338 $\times 10^{20}$
4 \rightarrow 5	.142770506 $\times 10^{-09}$.305813247 $\times 10^{00}$.645344607 $\times 10^{03}$.111449971 $\times 10^{08}$	-.144722005 $\times 10^{11}$.981325730 $\times 10^{13}$.381377623 $\times 10^{16}$.687380153 $\times 10^{18}$	-.529733459 $\times 10^{20}$
4 \rightarrow 6	.285584691 $\times 10^{-07}$	-.283108254 $\times 10^{00}$.509946612 $\times 10^{04}$.492454781 $\times 10^{07}$	-.552991649 $\times 10^{10}$.343706995 $\times 10^{13}$	-.121035857 $\times 10^{16}$.225460627 $\times 10^{18}$	-.172357375 $\times 10^{20}$
4 \rightarrow 7	.151393950 $\times 10^{-08}$	-.178162229 $\times 10^{-01}$.681878208 $\times 10^{04}$.469164476 $\times 10^{07}$	-.494055477 $\times 10^{10}$.289368287 $\times 10^{13}$	-.954910189 $\times 10^{15}$.166329763 $\times 10^{18}$	-.119009365 $\times 10^{20}$
4 \rightarrow 8	.289069740 $\times 10^{-10}$.347212105 $\times 10^{00}$.597384479 $\times 10^{04}$.915840770 $\times 10^{07}$	-.804969829 $\times 10^{10}$.390927059 $\times 10^{13}$	-.106579391 $\times 10^{16}$.151699928 $\times 10^{18}$	-.868345023 $\times 10^{19}$
4 \rightarrow 9	.266853727 $\times 10^{-09}$.992126968 $\times 10^{-01}$.997887556 $\times 10^{04}$.792022507 $\times 10^{06}$.362897467 $\times 10^{10}$	-.442551003 $\times 10^{13}$.215145119 $\times 10^{16}$	-.487422740 $\times 10^{18}$.425415380 $\times 10^{20}$
4 \rightarrow 10	.483801258 $\times 10^{-04}$	-.113775371 $\times 10^{01}$.224651039 $\times 10^{05}$	-.262515703 $\times 10^{08}$.352864767 $\times 10^{11}$.933263011 $\times 10^{14}$	-.183088111 $\times 10^{17}$.145316050 $\times 10^{21}$	
4 \rightarrow 11	.469907297 $\times 10^{-02}$	-.162429607 $\times 10^{01}$.263160975 $\times 10^{05}$	-.248811946 $\times 10^{08}$.256490646 $\times 10^{11}$	-.136601592 $\times 10^{14}$.377147121 $\times 10^{16}$	-.476144566 $\times 10^{18}$.169956977 $\times 10^{20}$
4 \rightarrow 12	.667577393 $\times 10^{-25}$.366464907 $\times 10^{01}$	-.240862894 $\times 10^{05}$.156895061 $\times 10^{09}$	-.275297247 $\times 10^{12}$.248346232 $\times 10^{15}$	-.119353375 $\times 10^{18}$.290127108 $\times 10^{20}$	-.280134488 $\times 10^{22}$
4 \rightarrow 13	.127413012 $\times 10^{-02}$	-.156757260 $\times 10^{01}$.262169127 $\times 10^{05}$	-.129742699 $\times 10^{08}$.582879017 $\times 10^{10}$.260297679 $\times 10^{13}$	-.351425186 $\times 10^{16}$.124796160 $\times 10^{19}$	-.152622058 $\times 10^{21}$
4 \rightarrow 14	.108973434 $\times 10^{-09}$.520516456 $\times 10^{-02}$.103397323 $\times 10^{05}$.497704000 $\times 10^{08}$	-.108082278 $\times 10^{12}$.114113901 $\times 10^{15}$	-.634032371 $\times 10^{17}$.177966350 $\times 10^{20}$	-.198748354 $\times 10^{22}$
4 \rightarrow 15	.138279259 $\times 10^{-06}$	-.759674291 $\times 10^{00}$.183347647 $\times 10^{05}$.201680455 $\times 10^{08}$	-.533540289 $\times 10^{11}$.617794959 $\times 10^{14}$	-.366778686 $\times 10^{17}$.109021544 $\times 10^{20}$	-.128456933 $\times 10^{22}$
4 \rightarrow 16	.472878576 $\times 10^{-05}$	-.120298291 $\times 10^{01}$.230990628 $\times 10^{05}$.162609913 $\times 10^{07}$	-.179807412 $\times 10^{11}$.266834604 $\times 10^{14}$	-.179116694 $\times 10^{17}$.579241462 $\times 10^{19}$	-.730775704 $\times 10^{21}$
5 \rightarrow 0	.464269548 $\times 10^{-04}$	-.955432236 $\times 10^{00}$.298544843 $\times 10^{04}$	-.611199941 $\times 10^{07}$.633710896 $\times 10^{10}$	-.373487864 $\times 10^{13}$.126430553 $\times 10^{16}$	-.228632566 $\times 10^{18}$.170942165 $\times 10^{20}$
5 \rightarrow 1	.964128192 $\times 10^{-04}$	-.102773143 $\times 10^{01}$.507911422 $\times 10^{04}$	-.106075515 $\times 10^{08}$.115480346 $\times 10^{11}$	-.720117954 $\times 10^{13}$.256480841 $\times 10^{16}$	-.483683729 $\times 10^{18}$.373993402 $\times 10^{20}$
5 \rightarrow 2	.774626050 $\times 10^{-08}$	-.927804503 $\times 10^{-04}$	-.307801868 $\times 10^{03}$	-.280120971 $\times 10^{07}$.637812655 $\times 10^{10}$	-.563346869 $\times 10^{13}$.245752043 $\times 10^{16}$	-.528424274 $\times 10^{18}$.447520014 $\times 10^{20}$
5 \rightarrow 3	.177679102 $\times 10^{-07}$	-.127971030 $\times 10^{00}$	-.283204197 $\times 10^{04}$.653832333 $\times 10^{07}$	-.713099231 $\times 10^{10}$.432973920 $\times 10^{13}$	-.149700975 $\times 10^{16}$.275194324 $\times 10^{18}$	-.208488663 $\times 10^{20}$
5 \rightarrow 4	.349159367 $\times 10^{-08}$.105101505 $\times 10^{00}$	-.347321305 $\times 10^{04}$.739517438 $\times 10^{07}$	-.800362565 $\times 10^{10}$.492768175 $\times 10^{13}$	-.173392540 $\times 10^{16}$.323758886 $\times 10^{18}$	-.248377156 $\times 10^{20}$
5 \rightarrow 5	.353043592 $\times 10^{-09}$.318593958 $\times 10^{00}$	-.149825970 $\times 10^{04}$.783364670 $\times 10^{07}$	-.818211016 $\times 10^{10}$.476183694 $\times 10^{13}$	-.157098492 $\times 10^{16}$.275323853 $\times 10^{18}$	-.199254819 $\times 10^{20}$
5 \rightarrow 6	.947077357 $\times 10^{-10}$.378309473 $\times 10^{00}$.771969123 $\times 10^{03}$.911207598 $\times 10^{07}$	-.108724939 $\times 10^{11}$.701556500 $\times 10^{13}$	-.250591357 $\times 10^{16}$.467090045 $\times 10^{18}$	-.354841746 $\times 10^{20}$
5 \rightarrow 7	.867711161 $\times 10^{-09}$.112416022 $\times 10^{00}$.453146107 $\times 10^{04}$.282036494 $\times 10^{07}$	-.179426386 $\times 10^{10}$.546887855 $\times 10^{12}$	-.494675944 $\times 10^{14}$	-.107317957 $\times 10^{17}$.200320660 $\times 10^{19}$
5 \rightarrow 8	.59999176 $\times 10^{-08}$	-.956219365 $\times 10^{-01}$.758647556 $\times 10^{04}$	-.476385005 $\times 10^{06}$.223540083 $\times 10^{10}$	-.211161829 $\times 10^{13}$.929455366 $\times 10^{15}$	-.199572873 $\times 10^{18}$.168524427 $\times 10^{20}$
5 \rightarrow 9	.588781689 $\times 10^{-09}$.112499951 $\times 10^{00}$.962254968 $\times 10^{04}$	-.256551450 $\times 10^{07}$.586373383 $\times 10^{10}$	-.511115448 $\times 10^{13}$.221166649 $\times 10^{16}$	-.473614265 $\times 10^{18}$.400399030 $\times 10^{20}$
5 \rightarrow 10	.222981753 $\times 10^{-09}$.173538548 $\times 10^{00}$.104097909 $\times 10^{05}$	-.241006322 $\times 10^{07}$.734414955 $\times 10^{10}$	-.683075001 $\times 10^{13}$.303166142 $\times 10^{16}$	-.657081319 $\times 10^{18}$.559066464 $\times 10^{20}$
5 \rightarrow 11	.139352815 $\times 10^{-07}$	-.277072938 $\times 10^{00}$.149710769 $\times 10^{05}$	-.108468418 $\times 10^{08}$.175982038 $\times 10^{11}$	-.135518137 $\times 10^{14}$.548116539 $\times 10^{16}$	-.112409120 $\times 10^{19}$.922062752 $\times 10^{20}$
5 \rightarrow 12	.122813403 $\times 10^{-04}$	-.993691128 $\times 10^{00}$.217471839 $\times 10^{05}$	-.234546208 $\times 10^{08}$.313561548 $\times 10^{11}$	-.218771040 $\times 10^{14}$.833007756 $\times 10^{16}$	-.163973723 $\times 10^{19}$.130552520 $\times 10^{21}$
5 \rightarrow 13	.270510715 $\times 10^{-03}$	-.134324766 $\times 10^{01}$.244791111 $\times 10^{05}$	-.244553684 $\times 10^{08}$.293683612 $\times 10^{11}$	-.187549882 $\times 10^{14}$.657144153 $\times 10^{16}$	-.118899510 $\times 10^{19}$.865294397 $\times 10^{20}$
5 \rightarrow 14	.276786202 $\times 10^{-07}$	-.458052074 $\times 10^{00}$.158661393 $\times 10^{05}$.973102564 $\times 10^{07}$	-.280557703 $\times 10^{11}$.314148667 $\times 10^{14}$	-.169579294 $\times 10^{17}$.441911455 $\times 10^{19}$	-.446013257 $\times 10^{21}$
5 \rightarrow 15	.403528694 $\times 10^{-21}$.273228297 $\times 10^{01}$	-.145432647 $\times 10^{05}$.118266905 $\times 10^{09}$	-.208063378 $\times 10^{12}$.188412564 $\times 10^{15}$	-.908119235 $\times 10^{17}$.221123266 $\times 10^{20}$	-.213641206 $\times 10^{22}$
5 \rightarrow 16	.480028370 $\times 10^{-24}$.333186075 $\times 10^{01}$	-.207337367 $\times 10^{05}$.144737990 $\times 10^{09}$	-.257671534 $\times 10^{12}$.237141249 $\times 10^{15}$	-.116571693 $\times 10^{18}$.290254390 $\times 10^{20}$	-.287346152 $\times 10^{22}$

Table 5 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH^+ ($v_i^+ = 6$ and 7) represented in the upper panels of Graph 5.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
6 \rightarrow 0	.101619967 $\times 10^{-05}$	-.617687637 $\times 10^{00}$.134770508 $\times 10^{04}$	-.245027759 $\times 10^{07}$.232350563 $\times 10^{10}$	-.134466407 $\times 10^{13}$.468395019 $\times 10^{15}$	-.890228309 $\times 10^{17}$.703466728 $\times 10^{19}$
6 \rightarrow 1	.265753802 $\times 10^{-02}$	-.134820531 $\times 10^{01}$.632322874 $\times 10^{04}$	-.140168179 $\times 10^{08}$.157316970 $\times 10^{11}$	-.985590430 $\times 10^{13}$.348499630 $\times 10^{16}$	-.649831258 $\times 10^{18}$.496519521 $\times 10^{20}$
6 \rightarrow 2	.880428656 $\times 10^{-06}$	-.527069495 $\times 10^{00}$.468191103 $\times 10^{04}$	-.178472039 $\times 10^{08}$.256601637 $\times 10^{11}$	-.185117478 $\times 10^{14}$.717228088 $\times 10^{16}$	-.114268616 $\times 10^{19}$.114268616 $\times 10^{21}$
6 \rightarrow 3	.883710078 $\times 10^{-07}$	-.310062285 $\times 10^{00}$	-.139559798 $\times 10^{04}$.335336275 $\times 10^{07}$	-.431735790 $\times 10^{10}$.303333006 $\times 10^{13}$	-.116883363 $\times 10^{16}$.232275162 $\times 10^{18}$	-.186163656 $\times 10^{20}$
6 \rightarrow 4	.809018782 $\times 10^{-11}$.633893753 $\times 10^{00}$	-.583317334 $\times 10^{04}$.147984046 $\times 10^{08}$	-.188219571 $\times 10^{11}$.126982896 $\times 10^{14}$	-.468766659 $\times 10^{16}$.896837888 $\times 10^{18}$	-.696135587 $\times 10^{20}$
6 \rightarrow 5	.241670141 $\times 10^{-09}$.358475784 $\times 10^{00}$	-.41406724 $\times 10^{04}$.848923943 $\times 10^{07}$	-.899468181 $\times 10^{10}$.531262744 $\times 10^{13}$.177839346 $\times 10^{16}$.316008073 $\times 10^{18}$	-.231644863 $\times 10^{20}$
6 \rightarrow 6	.879968218 $\times 10^{-08}$	-.274854872 $\times 10^{-01}$	-.3983662807 $\times 10^{03}$.455605247 $\times 10^{07}$	-.417876209 $\times 10^{10}$.223431647 $\times 10^{13}$	-.698025120 $\times 10^{15}$.118046686 $\times 10^{18}$	-.834216079 $\times 10^{19}$
6 \rightarrow 7	.326110002 $\times 10^{-08}$	-.186591568 $\times 10^{-01}$.206133293 $\times 10^{04}$.660108879 $\times 10^{07}$	-.939126275 $\times 10^{10}$.677694834 $\times 10^{13}$	-.261484551 $\times 10^{16}$.516143697 $\times 10^{18}$	-.410062542 $\times 10^{20}$
6 \rightarrow 8	.114041698 $\times 10^{-10}$.548419271 $\times 10^{00}$.290994093 $\times 10^{04}$.438435961 $\times 10^{07}$	-.284422996 $\times 10^{10}$.813736292 $\times 10^{12}$	-.221618049 $\times 10^{14}$	-.354450910 $\times 10^{17}$.517693052 $\times 10^{19}$
6 \rightarrow 9	.994128888 $\times 10^{-09}$.630153568 $\times 10^{-01}$.500661538 $\times 10^{04}$.423452042 $\times 10^{07}$	-.324946706 $\times 10^{10}$.136603213 $\times 10^{13}$.309373234 $\times 10^{15}$.330329736 $\times 10^{17}$	-.104312570 $\times 10^{19}$
6 \rightarrow 10	.603520032 $\times 10^{-08}$	-.124279346 $\times 10^{00}$.987160599 $\times 10^{04}$	-.476661850 $\times 10^{07}$.729759097 $\times 10^{10}$	-.616338387 $\times 10^{13}$.249068464 $\times 10^{16}$	-.510088855 $\times 10^{18}$	-.417924257 $\times 10^{20}$
6 \rightarrow 11	.436265811 $\times 10^{-08}$	-.122111232 $\times 10^{00}$.134952944 $\times 10^{05}$	-.123886916 $\times 10^{08}$.184983946 $\times 10^{11}$	-.136993206 $\times 10^{14}$.542116250 $\times 10^{16}$	-.109672303 $\times 10^{19}$.891378657 $\times 10^{20}$
6 \rightarrow 12	.251708647 $\times 10^{-08}$	-.108290473 $\times 10^{00}$.146597694 $\times 10^{05}$	-.134620824 $\times 10^{08}$.208470715 $\times 10^{11}$	-.157218758 $\times 10^{14}$.628770773 $\times 10^{16}$	-.128078542 $\times 10^{19}$.104598006 $\times 10^{21}$
6 \rightarrow 13	.200917883 $\times 10^{-07}$	-.363098261 $\times 10^{00}$.169600165 $\times 10^{05}$	-.160388078 $\times 10^{08}$.233272327 $\times 10^{11}$	-.170925530 $\times 10^{14}$.672949132 $\times 10^{16}$	-.135778715 $\times 10^{19}$.110194525 $\times 10^{21}$
6 \rightarrow 14	.276173734 $\times 10^{-06}$	-.680352860 $\times 10^{00}$.197240174 $\times 10^{05}$	-.199733910 $\times 10^{08}$.273468276 $\times 10^{11}$	-.194548939 $\times 10^{14}$.752647164 $\times 10^{16}$	-.150080668 $\times 10^{19}$.120760036 $\times 10^{21}$
6 \rightarrow 15	.201245417 $\times 10^{-05}$	-.916084042 $\times 10^{00}$.218267872 $\times 10^{05}$	-.233624164 $\times 10^{08}$.310269155 $\times 10^{11}$	-.216404541 $\times 10^{14}$.824713926 $\times 10^{16}$	-.162449389 $\times 10^{19}$.129354075 $\times 10^{21}$
6 \rightarrow 16	.484096543 $\times 10^{-05}$	-.108075824 $\times 10^{01}$.233575642 $\times 10^{05}$	-.258443735 $\times 10^{08}$.332475683 $\times 10^{11}$	-.225069947 $\times 10^{14}$.833338915 $\times 10^{16}$	-.159499830 $\times 10^{19}$.123321641 $\times 10^{21}$
7 \rightarrow 0	.344033843 $\times 10^{-07}$	-.343750066 $\times 10^{00}$	-.123560104 $\times 10^{04}$.359291755 $\times 10^{07}$	-.417940572 $\times 10^{10}$.251948583 $\times 10^{13}$	-.837107802 $\times 10^{15}$.145775341 $\times 10^{18}$	-.104082712 $\times 10^{20}$
7 \rightarrow 1	.101118469 $\times 10^{-01}$	-.154433132 $\times 10^{01}$.812426783 $\times 10^{04}$	-.178694792 $\times 10^{08}$.188027275 $\times 10^{11}$	-.109235576 $\times 10^{14}$.359590996 $\times 10^{16}$	-.629070925 $\times 10^{18}$.454583050 $\times 10^{20}$
7 \rightarrow 2	.250256450 $\times 10^{-04}$	-.977437717 $\times 10^{00}$.411594196 $\times 10^{04}$	-.611085641 $\times 10^{07}$.406495219 $\times 10^{10}$	-.151853092 $\times 10^{13}$.339947567 $\times 10^{15}$	-.441858887 $\times 10^{17}$.264538810 $\times 10^{19}$
7 \rightarrow 3	.281419847 $\times 10^{-08}$	-.567377937 $\times 10^{-01}$	-.361002382 $\times 10^{04}$.987598532 $\times 10^{07}$	-.114665911 $\times 10^{11}$.707654011 $\times 10^{13}$	-.244058359 $\times 10^{16}$.444140361 $\times 10^{18}$	-.332197670 $\times 10^{20}$
7 \rightarrow 4	.944119343 $\times 10^{-08}$	-.166703416 $\times 10^{00}$	-.278716947 $\times 10^{04}$.686178998 $\times 10^{07}$	-.792110711 $\times 10^{10}$.505290356 $\times 10^{13}$	-.181677527 $\times 10^{16}$.344046308 $\times 10^{18}$	-.266524646 $\times 10^{20}$
7 \rightarrow 5	.239998767 $\times 10^{-09}$.259324485 $\times 10^{00}$	-.374166360 $\times 10^{04}$.946888920 $\times 10^{07}$	-.116162559 $\times 10^{11}$.762166901 $\times 10^{13}$	-.275622784 $\times 10^{16}$.518959971 $\times 10^{18}$	-.397663753 $\times 10^{20}$
7 \rightarrow 6	.254878585 $\times 10^{-07}$	-.154604831 $\times 10^{00}$	-.197377626 $\times 10^{04}$.314126978 $\times 10^{07}$	-.259164237 $\times 10^{10}$.123610638 $\times 10^{13}$	-.342993457 $\times 10^{15}$.514286579 $\times 10^{17}$	-.322168370 $\times 10^{19}$
7 \rightarrow 7	.491790546 $\times 10^{-06}$	-.439808148 $\times 10^{00}$.136107997 $\times 10^{04}$.172796971 $\times 10^{07}$	-.182452580 $\times 10^{10}$.100681232 $\times 10^{13}$	-.308461533 $\times 10^{15}$.498348521 $\times 10^{17}$	-.331678018 $\times 10^{19}$
7 \rightarrow 8	.618784869 $\times 10^{-09}$.728224909 $\times 10^{-01}$.222151081 $\times 10^{03}$.849418717 $\times 10^{07}$	-.102401072 $\times 10^{11}$.681220289 $\times 10^{13}$	-.252398929 $\times 10^{16}$.487936460 $\times 10^{18}$	-.383464493 $\times 10^{20}$
7 \rightarrow 9	.167881292 $\times 10^{-07}$	-.224546096 $\times 10^{00}$.704840158 $\times 10^{04}$	-.487455242 $\times 10^{07}$.585892540 $\times 10^{10}$	-.377978932 $\times 10^{13}$.137353612 $\times 10^{16}$	-.263548439 $\times 10^{18}$.207152964 $\times 10^{20}$
7 \rightarrow 10	.298823760 $\times 10^{-09}$.136873040 $\times 10^{00}$.687213899 $\times 10^{04}$	-.306222945 $\times 10^{07}$.597243736 $\times 10^{10}$	-.491248736 $\times 10^{13}$.205911403 $\times 10^{16}$	-.431975931 $\times 10^{18}$.359925208 $\times 10^{20}$
7 \rightarrow 11	.366197038 $\times 10^{-07}$	-.381085338 $\times 10^{00}$.908668786 $\times 10^{04}$	-.317656898 $\times 10^{07}$.507413720 $\times 10^{10}$	-.390461579 $\times 10^{13}$.158155213 $\times 10^{16}$	-.324815600 $\times 10^{18}$.266731688 $\times 10^{20}$
7 \rightarrow 12	.688314135 $\times 10^{-07}$	-.464745271 $\times 10^{00}$.118293559 $\times 10^{05}$	-.770502349 $\times 10^{07}$.108276990 $\times 10^{11}$	-.779090977 $\times 10^{13}$.303038622 $\times 10^{16}$	-.605919670 $\times 10^{18}$.488237724 $\times 10^{20}$
7 \rightarrow 13	.314317080 $\times 10^{-07}$	-.429310844 $\times 10^{00}$.146892717 $\times 10^{05}$	-.140468792 $\times 10^{08}$.194719085 $\times 10^{11}$	-.138771593 $\times 10^{14}$.536107673 $\times 10^{16}$	-.106658578 $\times 10^{19}$.856199610 $\times 10^{20}$
7 \rightarrow 14	.185886699 $\times 10^{-07}$	-.431455198 $\times 10^{00}$.173143452 $\times 10^{05}$	-.207618564 $\times 10^{08}$.288500358 $\times 10^{11}$	-.205856069 $\times 10^{14}$.796172226 $\times 10^{16}$	-.158584409 $\times 10^{19}$.127453074 $\times 10^{21}$
7 \rightarrow 15	.153996525 $\times 10^{-08}$	-.217022559 $\times 10^{00}$.163361761 $\times 10^{05}$	-.175577877 $\times 10^{08}$.255730816 $\times 10^{11}$	-.187671835 $\times 10^{14}$.740062252 $\times 10^{16}$	-.149529307 $\times 10^{19}$.121496099 $\times 10^{21}$
7 \rightarrow 16	.110207180 $\times 10^{-09}$	-.294416999 $\times 10^{-01}$.145288474 $\times 10^{05}$	-.118140424 $\times 10^{08}$.187863397 $\times 10^{11}$	-.144586790 $\times 10^{14}$.587604405 $\times 10^{16}$	-.121198148 $\times 10^{19}$.999480375 $\times 10^{20}$

Table 6 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH^+ ($v_i^+ = 8$ and 9) represented in the upper panels of Graph 5.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
8 → 0	.184693578 × 10 ⁻⁰⁶	-.541917857 × 10 ⁰⁰	-.594213189 × 10 ⁰³	.148190306 × 10 ⁰⁷	-.132630145 × 10 ¹⁰	.582145197 × 10 ¹²	-.127196542 × 10 ¹⁵	.113530130 × 10 ¹⁷	-.800511948 × 10 ¹⁷
8 → 1	.323058068 × 10 ⁻⁰³	-.123015455 × 10 ⁰¹	.430770114 × 10 ⁰⁴	-.709124424 × 10 ⁰⁷	.572452855 × 10 ¹⁰	-.258979176 × 10 ¹³	.667954033 × 10 ¹⁵	-.913986871 × 10 ¹⁷	.511609551 × 10 ¹⁹
8 → 2	.134008508 × 10 ⁻⁰³	-.112344155 × 10 ⁰¹	.415557459 × 10 ⁰⁴	-.816462104 × 10 ⁰⁷	.900273264 × 10 ¹⁰	-.574711839 × 10 ¹³	.208695008 × 10 ¹⁶	-.399497593 × 10 ¹⁸	.312484365 × 10 ²⁰
8 → 3	.60566613 × 10 ⁻¹⁰	.334311293 × 10 ⁰⁰	-.441645243 × 10 ⁰⁴	.639486991 × 10 ⁰⁷	-.400570022 × 10 ¹⁰	.993028253 × 10 ¹²	.610314247 × 10 ¹⁴	-.718490612 × 10 ¹⁷	.920389754 × 10 ¹⁹
8 → 4	.156474286 × 10 ⁻⁰⁹	.275016049 × 10 ⁰⁰	-.383540503 × 10 ⁰⁴	.794359625 × 10 ⁰⁷	-.847158072 × 10 ¹⁰	.501189062 × 10 ¹³	-.170596928 × 10 ¹⁶	.305050575 × 10 ¹⁸	-.224454503 × 10 ²⁰
8 → 5	.165340301 × 10 ⁻⁰⁹	.287386106 × 10 ⁰⁰	-.321930128 × 10 ⁰⁴	.556874013 × 10 ⁰⁷	-.516219500 × 10 ¹⁰	.281259111 × 10 ¹³	-.898137202 × 10 ¹⁵	.155100090 × 10 ¹⁸	-.111617933 × 10 ²⁰
8 → 6	.135641643 × 10 ⁻⁰⁸	.737353369 × 10 ⁻⁰¹	-.279017625 × 10 ⁰⁴	.809507574 × 10 ⁰⁷	-.112360323 × 10 ¹¹	.802468844 × 10 ¹³	-.308411492 × 10 ¹⁶	.608133519 × 10 ¹⁸	-.483281683 × 10 ²⁰
8 → 7	.232761249 × 10 ⁻⁰⁶	-.351814469 × 10 ⁰⁰	-.142641059 × 10 ⁰⁴	.338307207 × 10 ⁰⁷	-.368805202 × 10 ¹⁰	.221212153 × 10 ¹³	-.752988831 × 10 ¹⁵	.136262909 × 10 ¹⁸	-.101746064 × 10 ²⁰
8 → 8	.293459040 × 10 ⁻⁰⁵	-.584429843 × 10 ⁰⁰	-.198485277 × 10 ⁰⁴	.608164196 × 10 ⁰⁵	.858893951 × 10 ⁰⁸	-.115685635 × 10 ¹²	.645573596 × 10 ¹⁴	-.160041352 × 10 ¹⁷	-.148198590 × 10 ¹⁹
8 → 9	.146043191 × 10 ⁻¹²	.923695021 × 10 ⁰⁰	-.638515589 × 10 ⁰⁴	.225572549 × 10 ⁰⁸	-.260012016 × 10 ¹¹	.167123475 × 10 ¹⁴	-.605079678 × 10 ¹⁶	.115212601 × 10 ¹⁹	-.896383666 × 10 ²⁰
8 → 10	.352925879 × 10 ⁻⁰⁸	-.816772987 × 10 ⁻⁰¹	.396584741 × 10 ⁰⁴	.987946514 × 10 ⁰⁶	-.282029978 × 10 ⁰⁹	-.128796089 × 10 ¹²	.118019188 × 10 ¹⁵	-.319024922 × 10 ¹⁷	.302229777 × 10 ¹⁹
8 → 11	.50839121 × 10 ⁻⁰⁹	.116421634 × 10 ⁰⁰	.696590241 × 10 ⁰⁴	-.492321135 × 10 ⁰⁷	.782999003 × 10 ¹⁰	-.585202267 × 10 ¹³	.231340339 × 10 ¹⁶	-.466621365 × 10 ¹⁸	.378120438 × 10 ²⁰
8 → 12	.330877487 × 10 ⁻¹⁰	.342495479 × 10 ⁰⁰	.550383748 × 10 ⁰⁴	.126525155 × 10 ⁰⁷	.994713956 × 10 ⁰⁹	-.167204691 × 10 ¹³	.868073100 × 10 ¹⁵	-.202228362 × 10 ¹⁸	.179345660 × 10 ²⁰
8 → 13	.100306299 × 10 ⁻⁰⁸	-.351565861 × 10 ⁻⁰¹	.738566250 × 10 ⁰⁴	.869039861 × 10 ⁰⁶	.335283140 × 10 ⁰⁹	-.818513619 × 10 ¹²	.459212723 × 10 ¹⁵	-.111345012 × 10 ¹⁸	.101300420 × 10 ²⁰
8 → 14	.193933257 × 10 ⁻⁰⁸	-.134457452 × 10 ⁰⁰	.892511896 × 10 ⁰⁴	-.918058974 × 10 ⁰⁶	.248661617 × 10 ¹⁰	-.228020025 × 10 ¹³	.101438668 × 10 ¹⁶	-.221097623 × 10 ¹⁸	.189189482 × 10 ²⁰
8 → 15	.757226897 × 10 ⁻⁰⁹	-.649270470 × 10 ⁻⁰¹	.958868637 × 10 ⁰⁴	-.172913516 × 10 ⁰⁷	.391735283 × 10 ¹⁰	-.343976512 × 10 ¹³	.149813000 × 10 ¹⁶	-.322282293 × 10 ¹⁸	.273302465 × 10 ²⁰
8 → 16	.590043926 × 10 ⁻¹⁰	.121413842 × 10 ⁰⁰	.956213721 × 10 ⁰⁴	-.173974683 × 10 ⁰⁷	.466259478 × 10 ¹⁰	-.425099621 × 10 ¹³	.188016919 × 10 ¹⁶	-.407837907 × 10 ¹⁸	.347683920 × 10 ²⁰
9 → 0	.104290438 × 10 ⁻⁰⁶	-.509020780 × 10 ⁰⁰	-.390441863 × 10 ⁰³	-.970904052 × 10 ⁰⁵	.129236370 × 10 ¹⁰	-.140290755 × 10 ¹³	.659432666 × 10 ¹⁵	-.146990112 × 10 ¹⁸	.127054508 × 10 ²⁰
9 → 1	.965709833 × 10 ⁻⁰⁴	-.114739201 × 10 ⁰¹	.217814802 × 10 ⁰⁴	-.140942040 × 10 ⁰⁷	-.412920973 × 10 ⁰⁹	.923996408 × 10 ¹²	-.460698877 × 10 ¹⁵	.101175266 × 10 ¹⁸	-.848980612 × 10 ¹⁹
9 → 2	.884446648 × 10 ⁻⁰⁴	-.110682310 × 10 ⁰¹	.361328633 × 10 ⁰⁴	-.822934254 × 10 ⁰⁷	.974073361 × 10 ¹⁰	-.636181483 × 10 ¹³	.232291728 × 10 ¹⁶	-.444235504 × 10 ¹⁸	.346376738 × 10 ²⁰
9 → 3	.351388332 × 10 ⁻⁰⁴	-.101939745 × 10 ⁰¹	.801402711 × 10 ⁰⁴	-.247624867 × 10 ⁰⁸	.324700657 × 10 ¹¹	-.222242915 × 10 ¹⁴	.832709313 × 10 ¹⁶	-.161810589 × 10 ¹⁹	.127519816 × 10 ²¹
9 → 4	.957678240 × 10 ⁻¹²	.760880998 × 10 ⁰⁰	-.641110628 × 10 ⁰⁴	.111915219 × 10 ⁰⁸	-.955616829 × 10 ¹⁰	.449349437 × 10 ¹³	-.117335862 × 10 ¹⁶	.156944303 × 10 ¹⁸	-.815605769 × 10 ¹⁹
9 → 5	.137882092 × 10 ⁻⁰⁸	.598522574 × 10 ⁻⁰¹	-.186470769 × 10 ⁰⁴	.190984388 × 10 ⁰⁷	-.666667597 × 10 ⁰⁹	-.170334919 × 10 ¹²	.205410871 × 10 ¹⁵	-.585611001 × 10 ¹⁷	.568724397 × 10 ¹⁹
9 → 6	.149459910 × 10 ⁻¹¹	.763117120 × 10 ⁰⁰	-.454140950 × 10 ⁰⁴	.770591884 × 10 ⁰⁷	-.689969271 × 10 ¹⁰	.353450231 × 10 ¹³	-.103907840 × 10 ¹⁶	.162914197 × 10 ¹⁸	-.105476976 × 10 ²⁰
9 → 7	.879933776 × 10 ⁻¹¹	.538974456 × 10 ⁰⁰	-.687881711 × 10 ⁰⁴	.155526030 × 10 ⁰⁸	-.180487813 × 10 ¹¹	.117266451 × 10 ¹⁴	-.428764764 × 10 ¹⁶	.822971346 × 10 ¹⁸	-.644382197 × 10 ²⁰
9 → 8	.259429922 × 10 ⁻⁰⁵	-.571476144 × 10 ⁰⁰	.606627130 × 10 ⁰²	.153403734 × 10 ⁰⁶	-.180587670 × 10 ⁰⁹	.654970671 × 10 ¹¹	-.383059989 × 10 ¹³	-.256558050 × 10 ¹⁶	.410649757 × 10 ¹⁸
9 → 9	.817696654 × 10 ⁻⁰⁵	-.663716128 × 10 ⁰⁰	.237770897 × 10 ⁰⁴	-.141656717 × 10 ⁰⁸	.162964384 × 10 ¹⁰	-.106974987 × 10 ¹³	.396449049 × 10 ¹⁵	-.770725717 × 10 ¹⁷	.610271396 × 10 ¹⁹
9 → 10	.389051185 × 10 ⁻¹¹	.615594634 × 10 ⁰⁰	-.360545553 × 10 ⁰⁴	.146792757 × 10 ⁰⁸	-.162682431 × 10 ¹¹	.101721230 × 10 ¹⁴	-.36028767 × 10 ¹⁶	.676810285 × 10 ¹⁸	-.520340624 × 10 ²⁰
9 → 11	.119707220 × 10 ⁻⁰⁸	-.501117028 × 10 ⁻⁰¹	.117259872 × 10 ⁰⁴	.770896304 × 10 ⁰⁷	-.877946700 × 10 ¹⁰	.559557789 × 10 ¹³	-.201441550 × 10 ¹⁶	.382087339 × 10 ¹⁸	-.296491027 × 10 ²⁰
9 → 12	.232654626 × 10 ⁻⁰⁸	-.778019409 × 10 ⁻⁰¹	.552542556 × 10 ⁰⁴	-.149863848 × 10 ⁰⁷	.299269714 × 10 ¹⁰	-.242610781 × 10 ¹³	.100054791 × 10 ¹⁶	-.207001944 × 10 ¹⁸	.170522956 × 10 ²⁰
9 → 13	.344743824 × 10 ⁻⁰⁹	.100653078 × 10 ⁰⁰	.727365897 × 10 ⁰⁴	-.411832635 × 10 ⁰⁷	.645338437 × 10 ¹⁰	-.482640500 × 10 ¹³	.191457836 × 10 ¹⁶	-.387426520 × 10 ¹⁸	.314726162 × 10 ²⁰
9 → 14	.398359743 × 10 ⁻¹⁰	.261962129 × 10 ⁰⁰	.639103069 × 10 ⁰⁴	-.372113965 × 10 ⁰⁵	.164326925 × 10 ¹⁰	-.175701543 × 10 ¹³	.822129735 × 10 ¹⁵	-.183382220 × 10 ¹⁸	.158893367 × 10 ²⁰
9 → 15	.661992936 × 10 ⁻¹⁰	.168463176 × 10 ⁰⁰	.622979118 × 10 ⁰⁴	.260762462 × 10 ⁰⁷	-.193191432 × 10 ¹⁰	.716992043 × 10 ¹²	-.111658606 × 10 ¹⁵	-.835007803 × 10 ¹⁸	.142876339 × 10 ¹⁹
9 → 16	.130875093 × 10 ⁻⁰⁹	.282599202 × 10 ⁻⁰¹	.695676289 × 10 ⁰⁴	.228244677 × 10 ⁰⁷	-.179647103 × 10 ¹⁰	.724990998 × 10 ¹²	-.138493983 × 10 ¹⁵	.758427615 × 10 ¹⁸	.581503239 × 10 ¹⁸

Table 7 List of the parameters used in Eq. (10) for the VE and VdE Maxwell rate coefficients of BeH^+ ($v_i^+ = 10$ and 11) represented in the upper panels of Graph. 5..

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
10 \rightarrow 0	.239260009 $\times 10^{-08}$	-.166440996 $\times 10^{00}$	-.158217399 $\times 10^{04}$.306325853 $\times 10^{06}$.242627010 $\times 10^{10}$	-.279953761 $\times 10^{13}$.133114147 $\times 10^{16}$	-.297670872 $\times 10^{18}$.257568692 $\times 10^{20}$
10 \rightarrow 1	.200920809 $\times 10^{-04}$	-.104032246 $\times 10^{01}$.672529357 $\times 10^{03}$.122771792 $\times 10^{07}$	-.260845095 $\times 10^{10}$.199582919 $\times 10^{13}$.177663734 $\times 10^{15}$	-.153200280 $\times 10^{18}$	-.121527192 $\times 10^{20}$
10 \rightarrow 2	.253113700 $\times 10^{-04}$	-.107473411 $\times 10^{01}$.235961091 $\times 10^{04}$	-.604270333 $\times 10^{07}$.729911578 $\times 10^{10}$	-.473924256 $\times 10^{13}$.170874712 $\times 10^{16}$	-.322545650 $\times 10^{18}$.248612252 $\times 10^{20}$
10 \rightarrow 3	.241112388 $\times 10^{-03}$	-.127906340 $\times 10^{01}$.818994846 $\times 10^{04}$	-.184785931 $\times 10^{08}$.201517061 $\times 10^{11}$	-.122904846 $\times 10^{14}$.425629668 $\times 10^{16}$	-.780786058 $\times 10^{18}$.588689596 $\times 10^{20}$
10 \rightarrow 4	.594023423 $\times 10^{-11}$.501656971 $\times 10^{00}$	-.521947559 $\times 10^{04}$.694513952 $\times 10^{06}$.384539190 $\times 10^{10}$.568077951 $\times 10^{12}$.291714829 $\times 10^{15}$	-.125708146 $\times 10^{18}$.139353132 $\times 10^{20}$
10 \rightarrow 5	.107506833 $\times 10^{-09}$.240313266 $\times 10^{00}$	-.173221041 $\times 10^{04}$.694820600 $\times 10^{06}$.150365129 $\times 10^{10}$	-.197192276 $\times 10^{13}$.974510463 $\times 10^{15}$	-.222430648 $\times 10^{18}$.195026894 $\times 10^{20}$
10 \rightarrow 6	.127860149 $\times 10^{-08}$	-.192237639 $\times 10^{-02}$	-.325340434 $\times 10^{04}$.603477943 $\times 10^{07}$.577625313 $\times 10^{10}$.319314677 $\times 10^{13}$.102650746 $\times 10^{16}$.177937107 $\times 10^{18}$	-.128433506 $\times 10^{20}$
10 \rightarrow 7	.291520464 $\times 10^{-08}$	-.427730062 $\times 10^{-01}$	-.348418348 $\times 10^{02}$	-.139402833 $\times 10^{07}$.204463434 $\times 10^{10}$	-.141118542 $\times 10^{13}$.531078547 $\times 10^{15}$	-.104233698 $\times 10^{18}$.832669938 $\times 10^{19}$
10 \rightarrow 8	.283861399 $\times 10^{-12}$.819669472 $\times 10^{00}$	-.993446758 $\times 10^{03}$.232000020 $\times 10^{08}$	-.271663798 $\times 10^{11}$.176546059 $\times 10^{14}$.644359605 $\times 10^{16}$	-.964886406 $\times 10^{20}$	
10 \rightarrow 9	.962896454 $\times 10^{-05}$	-.684634448 $\times 10^{00}$.789897418 $\times 10^{03}$	-.162942950 $\times 10^{07}$.189119518 $\times 10^{10}$	-.125047591 $\times 10^{13}$.466376404 $\times 10^{15}$	-.911737708 $\times 10^{17}$.725441244 $\times 10^{19}$
10 \rightarrow 10	.12456059 $\times 10^{-04}$	-.699443418 $\times 10^{00}$.232837982 $\times 10^{04}$	-.162870062 $\times 10^{07}$.179380571 $\times 10^{10}$	-.111554124 $\times 10^{13}$.393083498 $\times 10^{15}$	-.731620918 $\times 10^{17}$.558348721 $\times 10^{19}$
10 \rightarrow 11	.538038928 $\times 10^{-08}$	-.111795084 $\times 10^{00}$.803565224 $\times 10^{03}$.381106694 $\times 10^{07}$	-.371842189 $\times 10^{10}$.210616969 $\times 10^{13}$.690149963 $\times 10^{15}$.121156537 $\times 10^{18}$	-.880892650 $\times 10^{19}$
10 \rightarrow 12	.122900259 $\times 10^{-09}$.111583808 $\times 10^{00}$	-.147703867 $\times 10^{04}$.133411278 $\times 10^{08}$	-.156416865 $\times 10^{11}$.101360331 $\times 10^{14}$.368622489 $\times 10^{16}$.703795698 $\times 10^{18}$	-.548554551 $\times 10^{20}$
10 \rightarrow 13	.105823033 $\times 10^{-06}$	-.560988108 $\times 10^{00}$.530130563 $\times 10^{04}$	-.681638586 $\times 10^{06}$.101610475 $\times 10^{10}$.782106973 $\times 10^{12}$.320572720 $\times 10^{15}$	-.665403787 $\times 10^{17}$.550357874 $\times 10^{19}$
10 \rightarrow 14	.305003755 $\times 10^{-07}$	-.437813315 $\times 10^{00}$.679106361 $\times 10^{04}$	-.309616934 $\times 10^{07}$.421575735 $\times 10^{10}$	-.300822408 $\times 10^{13}$.116785246 $\times 10^{16}$	-.233406784 $\times 10^{18}$.188036589 $\times 10^{20}$
10 \rightarrow 15	.432594375 $\times 10^{-08}$	-.267165158 $\times 10^{00}$.732194979 $\times 10^{04}$	-.341460971 $\times 10^{07}$.478509776 $\times 10^{10}$	-.345644567 $\times 10^{13}$.134868194 $\times 10^{16}$	-.270040199 $\times 10^{18}$.217617494 $\times 10^{20}$
10 \rightarrow 16	.279854382 $\times 10^{-09}$	-.849433531 $\times 10^{-01}$.719787944 $\times 10^{04}$	-.223599623 $\times 10^{07}$.340831616 $\times 10^{10}$	-.259244811 $\times 10^{13}$.104717758 $\times 10^{16}$	-.214813539 $\times 10^{18}$.176197742 $\times 10^{20}$
11 \rightarrow 0	.136011216 $\times 10^{-07}$	-.365104235 $\times 10^{00}$	-.123760721 $\times 10^{03}$	-.273922179 $\times 10^{07}$.555639526 $\times 10^{10}$	-.459466599 $\times 10^{13}$.192040377 $\times 10^{16}$	-.401134528 $\times 10^{18}$.332869964 $\times 10^{20}$
11 \rightarrow 1	.180597558 $\times 10^{-04}$	-.103889058 $\times 10^{01}$.542476714 $\times 10^{03}$.545975488 $\times 10^{06}$	-.125993359 $\times 10^{10}$.979921501 $\times 10^{12}$	-.387193823 $\times 10^{15}$.775265933 $\times 10^{17}$	-.623414058 $\times 10^{19}$
11 \rightarrow 2	.310888631 $\times 10^{-04}$	-.110006666 $\times 10^{01}$.224017539 $\times 10^{04}$	-.345857979 $\times 10^{07}$.272188056 $\times 10^{10}$	-.119270863 $\times 10^{13}$.294436409 $\times 10^{15}$	-.378583309 $\times 10^{17}$.193051832 $\times 10^{19}$
11 \rightarrow 3	.756778276 $\times 10^{-03}$	-.137586330 $\times 10^{01}$.803756729 $\times 10^{04}$	-.181426766 $\times 10^{08}$.200166508 $\times 10^{11}$	-.122204105 $\times 10^{14}$.421537029 $\times 10^{16}$	-.769417577 $\times 10^{18}$.577490053 $\times 10^{20}$
11 \rightarrow 4	.211849306 $\times 10^{-04}$	-.997027500 $\times 10^{00}$.800406060 $\times 10^{04}$	-.254252787 $\times 10^{08}$.339252122 $\times 10^{11}$	-.234908067 $\times 10^{14}$.887272813 $\times 10^{16}$	-.173413215 $\times 10^{19}$.137249957 $\times 10^{21}$
11 \rightarrow 5	.713530761 $\times 10^{-11}$.540044405 $\times 10^{00}$	-.346127989 $\times 10^{04}$.267602295 $\times 10^{07}$.134330609 $\times 10^{10}$	-.290479714 $\times 10^{13}$.159163764 $\times 10^{16}$	-.380211678 $\times 10^{18}$.342050450 $\times 10^{20}$
11 \rightarrow 6	.799475322 $\times 10^{-09}$.898769425 $\times 10^{-01}$	-.763480860 $\times 10^{03}$	-.157457880 $\times 10^{07}$.412603183 $\times 10^{10}$	-.360310566 $\times 10^{13}$.153982043 $\times 10^{16}$	-.325489971 $\times 10^{18}$.272115551 $\times 10^{20}$
11 \rightarrow 7	.144710094 $\times 10^{-11}$.723180633 $\times 10^{00}$	-.475163940 $\times 10^{04}$.735588734 $\times 10^{07}$	-.605375749 $\times 10^{10}$.287932795 $\times 10^{13}$.788694214 $\times 10^{15}$.114977464 $\times 10^{18}$	-.687223581 $\times 10^{19}$
11 \rightarrow 8	.13686765 $\times 10^{-08}$.182758722 $\times 10^{-01}$	-.173776059 $\times 10^{04}$.259152563 $\times 10^{07}$	-.225715457 $\times 10^{10}$.120475462 $\times 10^{13}$	-.382865368 $\times 10^{15}$.661830585 $\times 10^{17}$	-.477809152 $\times 10^{19}$
11 \rightarrow 9	.131201737 $\times 10^{-11}$.729995594 $\times 10^{00}$	-.757014177 $\times 10^{04}$.165418653 $\times 10^{08}$	-.185755148 $\times 10^{11}$.117364212 $\times 10^{14}$	-.419863107 $\times 10^{16}$.792483316 $\times 10^{18}$	-.612496029 $\times 10^{20}$
11 \rightarrow 10	.129415976 $\times 10^{-04}$	-.700377613 $\times 10^{00}$.860023257 $\times 10^{03}$	-.185579485 $\times 10^{07}$.212910020 $\times 10^{10}$	-.137026489 $\times 10^{13}$.497183841 $\times 10^{15}$	-.948907372 $\times 10^{17}$.740017950 $\times 10^{19}$
11 \rightarrow 11	.156220083 $\times 10^{-04}$	-.715947087 $\times 10^{00}$.236081724 $\times 10^{04}$	-.226140509 $\times 10^{07}$.266784174 $\times 10^{10}$	-.173748886 $\times 10^{13}$.634095730 $\times 10^{15}$	-.121402477 $\times 10^{18}$.948512256 $\times 10^{19}$
11 \rightarrow 12	.141314660 $\times 10^{-06}$	-.411308474 $\times 10^{00}$.217720206 $\times 10^{04}$.258514061 $\times 10^{06}$.453663614 $\times 10^{08}$	-.150265640 $\times 10^{12}$.815394403 $\times 10^{14}$	-.190575770 $\times 10^{17}$.168458817 $\times 10^{19}$
11 \rightarrow 13	.565514376 $\times 10^{-10}$.255486296 $\times 10^{00}$	-.140058398 $\times 10^{04}$.108643583 $\times 10^{08}$	-.122331729 $\times 10^{11}$.773848680 $\times 10^{13}$	-.276978146 $\times 10^{16}$.522917074 $\times 10^{18}$	-.404216882 $\times 10^{20}$
11 \rightarrow 14	.234594100 $\times 10^{-08}$	-.224403408 $\times 10^{00}$.116808665 $\times 10^{04}$.803224582 $\times 10^{07}$	-.980061651 $\times 10^{10}$.650081257 $\times 10^{13}$	-.240103990 $\times 10^{16}$.463628712 $\times 10^{18}$	-.364542395 $\times 10^{20}$
11 \rightarrow 15	.265916145 $\times 10^{-07}$	-.489653364 $\times 10^{00}$.405505304 $\times 10^{04}$.242029772 $\times 10^{07}$	-.310814434 $\times 10^{10}$.209144297 $\times 10^{13}$	-.776288865 $\times 10^{15}$.150300136 $\times 10^{18}$	-.118440642 $\times 10^{20}$
11 \rightarrow 16	.585006259 $\times 10^{-08}$	-.385405170 $\times 10^{00}$.478554858 $\times 10^{04}$.111880351 $\times 10^{07}$	-.131960217 $\times 10^{10}$.830900309 $\times 10^{12}$	-.293294900 $\times 10^{15}$.547127124 $\times 10^{17}$	-.419466620 $\times 10^{19}$

Table 8 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH^+ ($v_i^+ = 12$ and 13) represented in the upper panels of Graph 6.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
12 \rightarrow 0	.187042454 $\times 10^{-07}$	-.434244052 $\times 10^{00}$.129070140 $\times 10^{04}$	-.645595864 $\times 10^{07}$.988158345 $\times 10^{10}$	-.735700671 $\times 10^{13}$.291366015 $\times 10^{16}$	-.589297290 $\times 10^{18}$.478758481 $\times 10^{20}$
12 \rightarrow 1	.218546493 $\times 10^{-05}$	-.862575293 $\times 10^{00}$	-.156338304 $\times 10^{03}$.119753753 $\times 10^{07}$	-.160555811 $\times 10^{10}$.109090375 $\times 10^{13}$	-.408485741 $\times 10^{15}$.797233097 $\times 10^{17}$	-.632365126 $\times 10^{19}$
12 \rightarrow 2	.156439995 $\times 10^{-04}$	-.106960560 $\times 10^{01}$.830822927 $\times 10^{03}$.708137951 $\times 10^{06}$	-.219644288 $\times 10^{10}$.186975782 $\times 10^{13}$	-.771866768 $\times 10^{15}$.158237466 $\times 10^{18}$	-.128970072 $\times 10^{20}$
12 \rightarrow 3	.204729003 $\times 10^{-03}$	-.128762785 $\times 10^{01}$.652952108 $\times 10^{04}$	-.139508435 $\times 10^{08}$.142323899 $\times 10^{11}$	-.808584851 $\times 10^{13}$.262454603 $\times 10^{16}$	-.455567245 $\times 10^{18}$.328070303 $\times 10^{20}$
12 \rightarrow 4	.356318115 $\times 10^{-02}$	-.154173331 $\times 10^{01}$.107318768 $\times 10^{05}$	-.265858922 $\times 10^{08}$.305484919 $\times 10^{11}$	-.191159723 $\times 10^{14}$.670564709 $\times 10^{16}$	-.123864929 $\times 10^{19}$.937772879 $\times 10^{20}$
12 \rightarrow 5	.464621774 $\times 10^{-09}$.859524853 $\times 10^{-01}$	-.209259772 $\times 10^{03}$	-.597458539 $\times 10^{07}$.119104614 $\times 10^{11}$	-.986002756 $\times 10^{13}$.413511505 $\times 10^{16}$	-.866485526 $\times 10^{18}$.720884936 $\times 10^{20}$
12 \rightarrow 6	.126685600 $\times 10^{-09}$.254710588 $\times 10^{00}$.569412935 $\times 10^{03}$	-.714909059 $\times 10^{07}$.123152178 $\times 10^{11}$	-.965412915 $\times 10^{13}$.393751444 $\times 10^{16}$	-.811490978 $\times 10^{18}$.667827077 $\times 10^{20}$
12 \rightarrow 7	.419325775 $\times 10^{-09}$.122407682 $\times 10^{00}$	-.252088065 $\times 10^{04}$.381886619 $\times 10^{07}$	-.294244216 $\times 10^{10}$.125962646 $\times 10^{13}$	-.295191167 $\times 10^{15}$.337380682 $\times 10^{17}$	-.129711913 $\times 10^{19}$
12 \rightarrow 8	.704749078 $\times 10^{-10}$.325238041 $\times 10^{00}$	-.785804566 $\times 10^{04}$	-.169752868 $\times 10^{07}$.390047618 $\times 10^{10}$	-.322027743 $\times 10^{13}$.133091622 $\times 10^{16}$	-.275130839 $\times 10^{18}$.226403172 $\times 10^{20}$
12 \rightarrow 9	.362586406 $\times 10^{-09}$.755960720 $\times 10^{-01}$	-.423920395 $\times 10^{04}$.976479528 $\times 10^{07}$	-.113260179 $\times 10^{11}$.732159967 $\times 10^{13}$	-.266448877 $\times 10^{16}$.509641184 $\times 10^{18}$	-.398083421 $\times 10^{20}$
12 \rightarrow 10	.117604349 $\times 10^{-08}$.603488545 $\times 10^{-01}$.310333909 $\times 10^{04}$.627036427 $\times 10^{07}$	-.674821040 $\times 10^{10}$.415421337 $\times 10^{13}$	-.146063310 $\times 10^{16}$.272314564 $\times 10^{18}$	-.208534404 $\times 10^{20}$
12 \rightarrow 11	.144257625 $\times 10^{-04}$	-.707573951 $\times 10^{00}$.934944627 $\times 10^{03}$	-.212184150 $\times 10^{07}$.24909751 $\times 10^{10}$	-.161943792 $\times 10^{13}$.589599781 $\times 10^{15}$	-.112674588 $\times 10^{18}$.879075450 $\times 10^{19}$
12 \rightarrow 13	.136752902 $\times 10^{-04}$	-.719253553 $\times 10^{00}$.212808563 $\times 10^{04}$	-.222721991 $\times 10^{07}$.268128018 $\times 10^{10}$	-.176347637 $\times 10^{13}$.647039368 $\times 10^{15}$	-.124283718 $\times 10^{18}$.973092726 $\times 10^{19}$
12 \rightarrow 14	.168053705 $\times 10^{-05}$	-.638552525 $\times 10^{00}$.281989507 $\times 10^{04}$	-.160121801 $\times 10^{07}$.193408102 $\times 10^{10}$	-.126870293 $\times 10^{13}$.464249953 $\times 10^{15}$	-.890139813 $\times 10^{17}$.696277152 $\times 10^{19}$
12 \rightarrow 15	.838425242 $\times 10^{-08}$	-.250802867 $\times 10^{00}$.142615989 $\times 10^{04}$.299869011 $\times 10^{07}$	-.324671558 $\times 10^{10}$.201567259 $\times 10^{13}$	-.713449945 $\times 10^{15}$.133634338 $\times 10^{18}$	-.102659434 $\times 10^{20}$
12 \rightarrow 16	.951916267 $\times 10^{-09}$	-.104278146 $\times 10^{00}$.506663451 $\times 10^{03}$.696583133 $\times 10^{07}$	-.816678729 $\times 10^{10}$.528941703 $\times 10^{13}$	-.192249626 $\times 10^{16}$.366921540 $\times 10^{18}$	-.285946585 $\times 10^{20}$
12 \rightarrow 17	.119920479 $\times 10^{-07}$	-.440596073 $\times 10^{00}$.256024928 $\times 10^{04}$.376995146 $\times 10^{07}$	-.479815660 $\times 10^{10}$.323598067 $\times 10^{13}$	-.120493266 $\times 10^{16}$.233732736 $\times 10^{18}$	-.184300198 $\times 10^{20}$
13 \rightarrow 0	.402546223 $\times 10^{-07}$	-.549774679 $\times 10^{00}$.245694284 $\times 10^{04}$	-.861855479 $\times 10^{07}$.118867242 $\times 10^{11}$	-.843228315 $\times 10^{13}$.325112283 $\times 10^{16}$	-.646706501 $\times 10^{18}$.519580383 $\times 10^{20}$
13 \rightarrow 1	.235502103 $\times 10^{-06}$	-.672968912 $\times 10^{00}$	-.460215942 $\times 10^{03}$.113655773 $\times 10^{07}$	-.121506086 $\times 10^{10}$.747696586 $\times 10^{12}$	-.265625214 $\times 10^{15}$.502293450 $\times 10^{17}$	-.390201486 $\times 10^{19}$
13 \rightarrow 2	.129760655 $\times 10^{-04}$	-.107984144 $\times 10^{01}$.271208715 $\times 10^{03}$.190816060 $\times 10^{07}$	-.338923434 $\times 10^{10}$.256286821 $\times 10^{13}$	-.100858683 $\times 10^{16}$.201903954 $\times 10^{18}$	-.162387193 $\times 10^{20}$
13 \rightarrow 3	.232974518 $\times 10^{-04}$	-.111934304 $\times 10^{01}$.387309664 $\times 10^{04}$	-.611406472 $\times 10^{07}$.475001674 $\times 10^{10}$	-.211013715 $\times 10^{13}$.547201642 $\times 10^{15}$	-.771990918 $\times 10^{17}$.458057047 $\times 10^{19}$
13 \rightarrow 4	.367014855 $\times 10^{-02}$	-.157124794 $\times 10^{01}$.100802602 $\times 10^{05}$	-.220654767 $\times 10^{08}$.230659949 $\times 10^{11}$	-.133477335 $\times 10^{14}$.438411558 $\times 10^{16}$	-.766019949 $\times 10^{18}$.553211425 $\times 10^{20}$
13 \rightarrow 5	.640076967 $\times 10^{-06}$	-.677011203 $\times 10^{00}$.571996687 $\times 10^{04}$	-.194662569 $\times 10^{08}$.268074281 $\times 10^{11}$	-.189824425 $\times 10^{14}$.729301767 $\times 10^{16}$	-.144446039 $\times 10^{19}$.115537822 $\times 10^{21}$
13 \rightarrow 6	.221183381 $\times 10^{-10}$.397188748 $\times 10^{00}$	-.150300176 $\times 10^{03}$	-.671420635 $\times 10^{07}$.129882856 $\times 10^{11}$	-.106309989 $\times 10^{14}$.443460199 $\times 10^{16}$	-.926627980 $\times 10^{18}$.769718084 $\times 10^{20}$
13 \rightarrow 7	.491635006 $\times 10^{-09}$.931217235 $\times 10^{-01}$	-.103147407 $\times 10^{04}$	-.673501038 $\times 10^{06}$.290438842 $\times 10^{10}$	-.277725830 $\times 10^{13}$.123830095 $\times 10^{16}$	-.268461797 $\times 10^{18}$.228247771 $\times 10^{20}$
13 \rightarrow 8	.215087322 $\times 10^{-11}$.631507996 $\times 10^{00}$	-.393024898 $\times 10^{04}$.568845361 $\times 10^{07}$	-.438403448 $\times 10^{10}$.192603799 $\times 10^{13}$	-.473955237 $\times 10^{15}$.591458741 $\times 10^{17}$	-.276123864 $\times 10^{19}$
13 \rightarrow 9	.688359620 $\times 10^{-09}$.506407665 $\times 10^{-01}$	-.107395623 $\times 10^{04}$.541304488 $\times 10^{06}$.487625881 $\times 10^{09}$	-.738344143 $\times 10^{12}$.367604264 $\times 10^{15}$	-.832015226 $\times 10^{17}$.721593412 $\times 10^{19}$
13 \rightarrow 10	.131370597 $\times 10^{-11}$.613406883 $\times 10^{00}$	-.827713931 $\times 10^{04}$.195546707 $\times 10^{08}$	-.230001321 $\times 10^{11}$.149890612 $\times 10^{14}$	-.548180369 $\times 10^{16}$.105184994 $\times 10^{19}$	-.823366465 $\times 10^{20}$
13 \rightarrow 11	.105990995 $\times 10^{-06}$	-.381063024 $\times 10^{00}$	-.575884372 $\times 10^{03}$.756957688 $\times 10^{06}$	-.575502478 $\times 10^{09}$.272311895 $\times 10^{12}$	-.781224365 $\times 10^{14}$.123505935 $\times 10^{17}$	-.822283999 $\times 10^{18}$
13 \rightarrow 12	.127228395 $\times 10^{-04}$	-.711669676 $\times 10^{00}$.892004372 $\times 10^{03}$	-.209530580 $\times 10^{07}$.251757634 $\times 10^{10}$	-.165212273 $\times 10^{13}$.604883933 $\times 10^{15}$	-.115962824 $\times 10^{18}$.906401556 $\times 10^{19}$
13 \rightarrow 14	.893190289 $\times 10^{-05}$	-.701348074 $\times 10^{00}$.179533548 $\times 10^{04}$	-.198861284 $\times 10^{07}$.24232757 $\times 10^{10}$	-.160327514 $\times 10^{13}$.590841966 $\times 10^{15}$	-.113966781 $\times 10^{18}$.893857154 $\times 10^{19}$
13 \rightarrow 15	.236712485 $\times 10^{-05}$	-.670757405 $\times 10^{00}$.245155671 $\times 10^{04}$	-.176006817 $\times 10^{07}$.211586928 $\times 10^{10}$	-.138934666 $\times 10^{13}$.509673170 $\times 10^{15}$	-.979526659 $\times 10^{17}$.767554839 $\times 10^{19}$
13 \rightarrow 16	.414411309 $\times 10^{-06}$	-.582320945 $\times 10^{00}$.256837572 $\times 10^{04}$	-.747525679 $\times 10^{06}$.914950137 $\times 10^{09}$	-.608345744 $\times 10^{12}$.225417176 $\times 10^{15}$	-.436984325 $\times 10^{17}$.345054652 $\times 10^{19}$
13 \rightarrow 17	.234315431 $\times 10^{-07}$	-.426973185 $\times 10^{00}$.201537342 $\times 10^{04}$.150912620 $\times 10^{07}$	-.176011927 $\times 10^{10}$.113298006 $\times 10^{13}$	-.409165757 $\times 10^{15}$.775914543 $\times 10^{17}$	-.600938664 $\times 10^{19}$

Table 9 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH⁺ ($v_e^+ = 14$ and 15) represented in the upper panels of Graph 6.

$v_e^+ \rightarrow v_f^+$	$A_{v_e^+ \rightarrow v_f^+}$	$\alpha_{v_e^+ \rightarrow v_f^+}$	$B_{v_e^+ \rightarrow v_f^+}(1)$	$B_{v_e^+ \rightarrow v_f^+}(2)$	$B_{v_e^+ \rightarrow v_f^+}(3)$	$B_{v_e^+ \rightarrow v_f^+}(4)$	$B_{v_e^+ \rightarrow v_f^+}(5)$	$B_{v_e^+ \rightarrow v_f^+}(6)$	$B_{v_e^+ \rightarrow v_f^+}(7)$
14 \rightarrow 0	.746501579 $\times 10^{-07}$	-.663810453 $\times 10^{00}$.272685985 $\times 10^{04}$	-.791362284 $\times 10^{07}$.101716673 $\times 10^{11}$	-.698198911 $\times 10^{13}$.264496539 $\times 10^{16}$	-.520698183 $\times 10^{18}$.415595050 $\times 10^{20}$
14 \rightarrow 1	.648276362 $\times 10^{-07}$	-.588342904 $\times 10^{00}$	-.238045874 $\times 10^{03}$.367576608 $\times 10^{06}$	-.316838382 $\times 10^{09}$.172543203 $\times 10^{12}$	-.560440472 $\times 10^{14}$.978769015 $\times 10^{16}$	-.704828271 $\times 10^{18}$
14 \rightarrow 2	.861241840 $\times 10^{-05}$	-.107872527 $\times 10^{01}$.787319623 $\times 10^{02}$.200388835 $\times 10^{06}$	-.334888956 $\times 10^{10}$.250143691 $\times 10^{13}$	-.981945492 $\times 10^{15}$.196631318 $\times 10^{18}$	-.158329023 $\times 10^{20}$
14 \rightarrow 3	.890745457 $\times 10^{-05}$	-.107651403 $\times 10^{01}$.227867903 $\times 10^{04}$	-.250497022 $\times 10^{07}$.130409507 $\times 10^{10}$	-.30635357 $\times 10^{12}$.324675891 $\times 10^{13}$.117450359 $\times 10^{17}$	-.153259798 $\times 10^{19}$
14 \rightarrow 4	.932853710 $\times 10^{-04}$	-.147201544 $\times 10^{01}$.878564114 $\times 10^{04}$	-.171341106 $\times 10^{08}$.160118156 $\times 10^{11}$	-.836155976 $\times 10^{13}$.250280121 $\times 10^{16}$	-.402109207 $\times 10^{18}$.269159361 $\times 10^{20}$
14 \rightarrow 5	.529868835 $\times 10^{-04}$	-.116360774 $\times 10^{01}$.853351599 $\times 10^{04}$	-.237273211 $\times 10^{08}$.297376803 $\times 10^{11}$	-.198853414 $\times 10^{14}$.743439404 $\times 10^{16}$	-.413000588 $\times 10^{19}$.110533674 $\times 10^{21}$
14 \rightarrow 6	.165702336 $\times 10^{-09}$.150055712 $\times 10^{00}$.11539285 $\times 10^{04}$	-.935542669 $\times 10^{07}$.156055638 $\times 10^{11}$	-.121191790 $\times 10^{14}$.492706648 $\times 10^{16}$	-.101448656 $\times 10^{19}$.834875272 $\times 10^{20}$
14 \rightarrow 7	.697761908 $\times 10^{-10}$.265486975 $\times 10^{00}$.178387505 $\times 10^{03}$	-.554758901 $\times 10^{07}$.100463328 $\times 10^{11}$	-.804861984 $\times 10^{13}$.332507905 $\times 10^{16}$	-.691083393 $\times 10^{18}$.572098565 $\times 10^{20}$
14 \rightarrow 8	.115119808 $\times 10^{-09}$.193713644 $\times 10^{00}$	-.266575328 $\times 10^{04}$.438473483 $\times 10^{07}$	-.394409039 $\times 10^{10}$.204579794 $\times 10^{13}$	-.609563501 $\times 10^{15}$.968778428 $\times 10^{17}$	-.636176317 $\times 10^{19}$
14 \rightarrow 9	.339565319 $\times 10^{-10}$.345662446 $\times 10^{00}$	-.104315883 $\times 10^{04}$	-.350087407 $\times 10^{06}$.186638751 $\times 10^{10}$.175580870 $\times 10^{13}$.768616801 $\times 10^{15}$	-.164115274 $\times 10^{18}$.137812333 $\times 10^{20}$
14 \rightarrow 10	.373999656 $\times 10^{-08}$	-.198466429 $\times 10^{00}$	-.186434481 $\times 10^{04}$.413992274 $\times 10^{07}$	-.471078521 $\times 10^{10}$.299935160 $\times 10^{13}$	-.107887480 $\times 10^{16}$.204619128 $\times 10^{18}$	-.158877117 $\times 10^{20}$
14 \rightarrow 11	.153110726 $\times 10^{-10}$.392970371 $\times 10^{00}$	-.585254757 $\times 10^{04}$.131134603 $\times 10^{08}$	-.150208930 $\times 10^{11}$.962894270 $\times 10^{13}$	-.348205822 $\times 10^{16}$.662717919 $\times 10^{18}$	-.515587500 $\times 10^{20}$
14 \rightarrow 12	.141540134 $\times 10^{-05}$	-.620501556 $\times 10^{00}$.521415857 $\times 10^{03}$	-.130126789 $\times 10^{07}$.156213890 $\times 10^{10}$	-.101626245 $\times 10^{13}$.369044566 $\times 10^{15}$	-.703095565 $\times 10^{17}$.547127927 $\times 10^{19}$
14 \rightarrow 13	.838744206 $\times 10^{-05}$	-.694744516 $\times 10^{00}$.757153235 $\times 10^{03}$	-.187850997 $\times 10^{07}$.228449958 $\times 10^{10}$	-.150919422 $\times 10^{13}$.555243641 $\times 10^{15}$	-.106860829 $\times 10^{18}$.837954381 $\times 10^{19}$
14 \rightarrow 15	.520712941 $\times 10^{-05}$	-.662845161 $\times 10^{00}$.142264372 $\times 10^{04}$	-.169884215 $\times 10^{07}$.206196723 $\times 10^{10}$	-.136504112 $\times 10^{13}$.504106405 $\times 10^{15}$	-.973956726 $\times 10^{17}$.766372135 $\times 10^{19}$
14 \rightarrow 16	.193921683 $\times 10^{-05}$	-.652140936 $\times 10^{00}$.202071152 $\times 10^{04}$	-.179284794 $\times 10^{07}$.215666287 $\times 10^{10}$	-.142723727 $\times 10^{13}$.527755148 $\times 10^{15}$	-.102102062 $\times 10^{18}$.804313042 $\times 10^{19}$
14 \rightarrow 17	.348570361 $\times 10^{-06}$	-.600779646 $\times 10^{00}$.217320510 $\times 10^{04}$	-.120502974 $\times 10^{07}$.145050618 $\times 10^{10}$	-.966287250 $\times 10^{12}$.359605005 $\times 10^{15}$	-.699522837 $\times 10^{17}$.553582956 $\times 10^{19}$
15 \rightarrow 0	.697677439 $\times 10^{-07}$	-.719647983 $\times 10^{00}$.248761552 $\times 10^{04}$	-.653204998 $\times 10^{07}$.805116512 $\times 10^{10}$	-.540960167 $\times 10^{13}$.202482592 $\times 10^{16}$	-.395741562 $\times 10^{18}$.314412214 $\times 10^{20}$
15 \rightarrow 1	.166190588 $\times 10^{-07}$	-.511037284 $\times 10^{00}$	-.471678228 $\times 10^{03}$.104385537 $\times 10^{07}$	-.113002589 $\times 10^{10}$.671956941 $\times 10^{12}$	-.223761869 $\times 10^{15}$.391947354 $\times 10^{17}$	-.281448250 $\times 10^{19}$
15 \rightarrow 2	.376249706 $\times 10^{-05}$	-.104862689 $\times 10^{01}$.229140151 $\times 10^{02}$.193035471 $\times 10^{07}$	-.321125532 $\times 10^{10}$.241065558 $\times 10^{13}$	-.951348108 $\times 10^{15}$.191360464 $\times 10^{18}$	-.154644086 $\times 10^{20}$
15 \rightarrow 3	.68008480 $\times 10^{-05}$	-.110624458 $\times 10^{01}$.162530538 $\times 10^{04}$	-.124169217 $\times 10^{07}$.121924675 $\times 10^{09}$.355295166 $\times 10^{12}$	-.218580257 $\times 10^{15}$.523469424 $\times 10^{17}$	-.463407900 $\times 10^{19}$
15 \rightarrow 4	.139248342 $\times 10^{-03}$	-.133384507 $\times 10^{01}$.737511753 $\times 10^{04}$	-.130987755 $\times 10^{08}$.114560786 $\times 10^{11}$	-.573488708 $\times 10^{13}$.167515600 $\times 10^{16}$	-.266045207 $\times 10^{18}$.177657646 $\times 10^{20}$
15 \rightarrow 5	.213673288 $\times 10^{-03}$	-.135032917 $\times 10^{01}$.924121533 $\times 10^{04}$	-.240480646 $\times 10^{08}$.288686168 $\times 10^{11}$	-.186984035 $\times 10^{14}$.673992166 $\times 10^{16}$	-.127239811 $\times 10^{19}$.980569405 $\times 10^{20}$
15 \rightarrow 6	.322397358 $\times 10^{-08}$	-.2034447735 $\times 10^{00}$.342209639 $\times 10^{04}$	-.139371986 $\times 10^{08}$.204386469 $\times 10^{11}$	-.150400592 $\times 10^{14}$.593683383 $\times 10^{16}$	-.119977971 $\times 10^{19}$.974573333 $\times 10^{20}$
15 \rightarrow 7	.144154791 $\times 10^{-10}$.385784906 $\times 10^{00}$.129162423 $\times 10^{04}$	-.106050639 $\times 10^{08}$.177910908 $\times 10^{11}$	-.138857242 $\times 10^{14}$.566437067 $\times 10^{16}$	-.116879721 $\times 10^{19}$.963156769 $\times 10^{20}$
15 \rightarrow 8	.213486936 $\times 10^{-09}$.990933461 $\times 10^{-01}$	-.188920232 $\times 10^{04}$.261242340 $\times 10^{07}$	-.179016060 $\times 10^{10}$.572416389 $\times 10^{12}$	-.472737377 $\times 10^{14}$	-.146688597 $\times 10^{17}$.259440510 $\times 10^{19}$
15 \rightarrow 9	.189157381 $\times 10^{-11}$.584264689 $\times 10^{00}$	-.315453096 $\times 10^{04}$.483856733 $\times 10^{07}$	-.433238439 $\times 10^{10}$.223588635 $\times 10^{13}$	-.665881959 $\times 10^{15}$.106236726 $\times 10^{18}$	-.703174912 $\times 10^{19}$
15 \rightarrow 10	.129991172 $\times 10^{-08}$	-.956439541 $\times 10^{-01}$	-.101658953 $\times 10^{04}$.148943871 $\times 10^{07}$	-.125237872 $\times 10^{10}$.616020479 $\times 10^{12}$	-.177484015 $\times 10^{15}$.278996444 $\times 10^{17}$	-.185211601 $\times 10^{19}$
15 \rightarrow 11	.474324711 $\times 10^{-09}$	-.562573103 $\times 10^{-01}$	-.423610992 $\times 10^{04}$.107983678 $\times 10^{08}$	-.132344260 $\times 10^{11}$.883207292 $\times 10^{13}$	-.328019329 $\times 10^{16}$.636309306 $\times 10^{18}$	-.502189402 $\times 10^{20}$
15 \rightarrow 12	.477012556 $\times 10^{-08}$	-.191493163 $\times 10^{00}$	-.189293499 $\times 10^{04}$.398022972 $\times 10^{07}$	-.446496627 $\times 10^{10}$.284303212 $\times 10^{13}$	-.102557406 $\times 10^{16}$.194959236 $\times 10^{18}$	-.151554092 $\times 10^{20}$
15 \rightarrow 13	.209454925 $\times 10^{-05}$	-.657898512 $\times 10^{00}$.625107587 $\times 10^{03}$	-.154733204 $\times 10^{07}$.185113896 $\times 10^{10}$	-.120949669 $\times 10^{13}$.441875768 $\times 10^{15}$	-.846508026 $\times 10^{17}$.661696772 $\times 10^{19}$
15 \rightarrow 14	.496320636 $\times 10^{-05}$	-.657804922 $\times 10^{00}$.643315833 $\times 10^{03}$	-.161639512 $\times 10^{07}$.195846962 $\times 10^{10}$	-.129454316 $\times 10^{13}$.477516910 $\times 10^{15}$	-.921794293 $\times 10^{17}$.724870954 $\times 10^{19}$
15 \rightarrow 16	.415983695 $\times 10^{-05}$	-.620586406 $\times 10^{00}$.110353922 $\times 10^{04}$	-.137520679 $\times 10^{07}$.165651516 $\times 10^{10}$	-.109963333 $\times 10^{13}$.407965232 $\times 10^{15}$	-.791610939 $\times 10^{17}$.625138359 $\times 10^{19}$
15 \rightarrow 17	.838848752 $\times 10^{-06}$	-.609224426 $\times 10^{00}$.155851052 $\times 10^{04}$	-.156159335 $\times 10^{07}$.190337169 $\times 10^{10}$	-.127706622 $\times 10^{13}$.477394616 $\times 10^{15}$	-.931297516 $\times 10^{17}$.738332010 $\times 10^{19}$

Table 10 List of the parameters used in Eq.(10) for the VE and VdE Maxwell rate coefficients of BeH⁺ (v_i^+ = 16 and 17) represented in the upper panels of Graph 6.

$v_i^+ \rightarrow v_f^+$	$A_{v_i^+ \rightarrow v_f^+}$	$\alpha_{v_i^+ \rightarrow v_f^+}$	$B_{v_i^+ \rightarrow v_f^+}(1)$	$B_{v_i^+ \rightarrow v_f^+}(2)$	$B_{v_i^+ \rightarrow v_f^+}(3)$	$B_{v_i^+ \rightarrow v_f^+}(4)$	$B_{v_i^+ \rightarrow v_f^+}(5)$	$B_{v_i^+ \rightarrow v_f^+}(6)$	$B_{v_i^+ \rightarrow v_f^+}(7)$
16 \rightarrow 0	.760415137 $\times 10^{-07}$	-.781552211 $\times 10^{00}$.362270227 $\times 10^{04}$	-.864034487 $\times 10^{07}$.992100746 $\times 10^{10}$	-.635687548 $\times 10^{13}$.230529156 $\times 10^{16}$	-.440949132 $\times 10^{18}$.345064186 $\times 10^{20}$
16 \rightarrow 1	.944911316 $\times 10^{-09}$	-.277153578 $\times 10^{00}$	-.125580357 $\times 10^{04}$.222446721 $\times 10^{07}$	-.205720792 $\times 10^{10}$.105966910 $\times 10^{13}$	-.307029813 $\times 10^{15}$.466655684 $\times 10^{17}$	-.288319559 $\times 10^{19}$
16 \rightarrow 2	.147592850 $\times 10^{-06}$	-.795476782 $\times 10^{00}$	-.125105379 $\times 10^{04}$.455817442 $\times 10^{07}$	-.612779263 $\times 10^{10}$.426089685 $\times 10^{13}$	-.161937603 $\times 10^{16}$.318740427 $\times 10^{18}$	-.254049000 $\times 10^{20}$
16 \rightarrow 3	.224210589 $\times 10^{-05}$	-.107397045 $\times 10^{01}$.836517193 $\times 10^{03}$.749348278 $\times 10^{06}$	-.225072475 $\times 10^{10}$.191470873 $\times 10^{13}$	-.793679766 $\times 10^{15}$.163566913 $\times 10^{18}$	-.134008894 $\times 10^{20}$
16 \rightarrow 4	.152753881 $\times 10^{-04}$	-.120048163 $\times 10^{01}$.609033767 $\times 10^{04}$	-.101974745 $\times 10^{08}$.862664644 $\times 10^{10}$	-.425592934 $\times 10^{13}$.124042990 $\times 10^{16}$	-.198132691 $\times 10^{18}$.133707182 $\times 10^{20}$
16 \rightarrow 5	.238270575 $\times 10^{-03}$	-.144261430 $\times 10^{01}$.964504824 $\times 10^{04}$	-.244726088 $\times 10^{08}$.287529593 $\times 10^{11}$	-.182800059 $\times 10^{14}$.648650802 $\times 10^{16}$	-.120864113 $\times 10^{19}$.921340693 $\times 10^{20}$
16 \rightarrow 6	.628655177 $\times 10^{-08}$	-.360336847 $\times 10^{00}$.364374872 $\times 10^{04}$	-.129474293 $\times 10^{08}$.183344389 $\times 10^{11}$	-.133011993 $\times 10^{14}$.521090029 $\times 10^{16}$	-.104784757 $\times 10^{19}$.848146955 $\times 10^{20}$
16 \rightarrow 7	.365589959 $\times 10^{-11}$.427961200 $\times 10^{00}$.637630348 $\times 10^{03}$	-.902980296 $\times 10^{07}$.157320993 $\times 10^{11}$	-.124327742 $\times 10^{14}$.510564535 $\times 10^{16}$	-.105822515 $\times 10^{19}$.874926424 $\times 10^{20}$
16 \rightarrow 8	.103270094 $\times 10^{-08}$	-.137237277 $\times 10^{00}$	-.535837465 $\times 10^{03}$	-.456237063 $\times 10^{06}$.185890013 $\times 10^{10}$	-.182730013 $\times 10^{13}$.832471581 $\times 10^{15}$	-.183135375 $\times 10^{18}$.157246083 $\times 10^{20}$
16 \rightarrow 9	.508117055 $\times 10^{-10}$.160826340 $\times 10^{00}$	-.233973574 $\times 10^{04}$.446201178 $\times 10^{06}$	-.456311834 $\times 10^{10}$.263700603 $\times 10^{13}$	-.870449528 $\times 10^{15}$.153299779 $\times 10^{18}$	-.111753709 $\times 10^{20}$
16 \rightarrow 10	.101329196 $\times 10^{-08}$	-.114356466 $\times 10^{00}$	-.444405893 $\times 10^{02}$	-.922111483 $\times 10^{06}$.170281938 $\times 10^{10}$	-.137091868 $\times 10^{13}$.564664102 $\times 10^{15}$	-.116507060 $\times 10^{18}$.955865288 $\times 10^{19}$
16 \rightarrow 11	.157196152 $\times 10^{-06}$	-.688968392 $\times 10^{00}$.182492069 $\times 10^{03}$.477582601 $\times 10^{06}$	-.100267776 $\times 10^{10}$.788265533 $\times 10^{12}$	-.316094170 $\times 10^{15}$.641935893 $\times 10^{17}$	-.523014787 $\times 10^{19}$
16 \rightarrow 12	.155918954 $\times 10^{-08}$	-.172323387 $\times 10^{00}$	-.285137298 $\times 10^{03}$.705976366 $\times 10^{06}$	-.851776768 $\times 10^{10}$.562445047 $\times 10^{12}$	-.207272784 $\times 10^{15}$.399681413 $\times 10^{18}$	-.313939696 $\times 10^{20}$
16 \rightarrow 13	.519634595 $\times 10^{-06}$	-.610832854 $\times 10^{00}$.394457059 $\times 10^{03}$	-.919324729 $\times 10^{06}$.107121318 $\times 10^{10}$	-.689898128 $\times 10^{12}$.249949263 $\times 10^{15}$	-.476590371 $\times 10^{17}$.371661038 $\times 10^{19}$
16 \rightarrow 14	.211446024 $\times 10^{-05}$	-.663219782 $\times 10^{00}$.779220715 $\times 10^{03}$	-.185780461 $\times 10^{07}$.221534182 $\times 10^{10}$	-.145799380 $\times 10^{13}$.537100955 $\times 10^{15}$	-.103631905 $\times 10^{18}$.814763361 $\times 10^{19}$
16 \rightarrow 15	.417906356 $\times 10^{-05}$	-.621577343 $\times 10^{00}$.567456125 $\times 10^{03}$	-.136230446 $\times 10^{07}$.163617349 $\times 10^{10}$	-.108422735 $\times 10^{13}$.401841750 $\times 10^{15}$	-.779311181 $\times 10^{17}$.615291156 $\times 10^{19}$
16 \rightarrow 17	.209393075 $\times 10^{-05}$	-.544249202 $\times 10^{00}$.550239416 $\times 10^{03}$	-.354579185 $\times 10^{06}$.388082520 $\times 10^{09}$	-.242389235 $\times 10^{12}$.860788705 $\times 10^{14}$	-.161470837 $\times 10^{17}$.124036973 $\times 10^{19}$
17 \rightarrow 0	.175028809 $\times 10^{-07}$	-.728297818 $\times 10^{00}$.185198605 $\times 10^{04}$	-.523070042 $\times 10^{07}$.670597961 $\times 10^{10}$	-.458619850 $\times 10^{13}$.172996498 $\times 10^{16}$	-.339215350 $\times 10^{18}$.269826496 $\times 10^{20}$
17 \rightarrow 1	.481074014 $\times 10^{-08}$	-.530547304 $\times 10^{00}$	-.799049964 $\times 10^{03}$.227732612 $\times 10^{07}$	-.273387283 $\times 10^{10}$.174293293 $\times 10^{13}$	-.616268992 $\times 10^{15}$.114125382 $\times 10^{18}$	-.863737285 $\times 10^{19}$
17 \rightarrow 2	.151072659 $\times 10^{-05}$	-.107289441 $\times 10^{01}$.668207350 $\times 10^{03}$.346502285 $\times 10^{06}$	-.137995509 $\times 10^{10}$.124478010 $\times 10^{13}$	-.533654522 $\times 10^{15}$.112536952 $\times 10^{18}$	-.937537528 $\times 10^{19}$
17 \rightarrow 3	.396687603 $\times 10^{-05}$	-.116924351 $\times 10^{01}$.153073527 $\times 10^{04}$	-.119165944 $\times 10^{07}$.164296123 $\times 10^{09}$.312296308 $\times 10^{12}$	-.204285276 $\times 10^{15}$.502892036 $\times 10^{17}$	-.453166625 $\times 10^{19}$
17 \rightarrow 4	.125127638 $\times 10^{-04}$	-.121222953 $\times 10^{01}$.607752674 $\times 10^{04}$	-.115176193 $\times 10^{08}$.112815570 $\times 10^{11}$	-.641324511 $\times 10^{13}$.212129157 $\times 10^{16}$	-.377746788 $\times 10^{18}$.279429368 $\times 10^{20}$
17 \rightarrow 5	.210023980 $\times 10^{-03}$	-.145471487 $\times 10^{01}$.947653966 $\times 10^{04}$	-.224747560 $\times 10^{08}$.252250229 $\times 10^{11}$	-.155604504 $\times 10^{14}$.540981619 $\times 10^{16}$	-.993706848 $\times 10^{18}$.749715792 $\times 10^{20}$
17 \rightarrow 6	.205013127 $\times 10^{-06}$	-.738462409 $\times 10^{00}$.711345185 $\times 10^{04}$	-.224877944 $\times 10^{08}$.300982892 $\times 10^{11}$	-.209930978 $\times 10^{14}$.798840223 $\times 10^{16}$	-.157158798 $\times 10^{19}$.125082854 $\times 10^{21}$
17 \rightarrow 7	.896365410 $\times 10^{-12}$.559656752 $\times 10^{00}$.120016505 $\times 10^{03}$	-.883960728 $\times 10^{07}$.169008018 $\times 10^{11}$	-.139572341 $\times 10^{14}$.588149475 $\times 10^{16}$	-.123955551 $\times 10^{19}$.103673078 $\times 10^{21}$
17 \rightarrow 8	.195231136 $\times 10^{-11}$.483310051 $\times 10^{00}$	-.290894447 $\times 10^{04}$.349878056 $\times 10^{07}$	-.159828963 $\times 10^{10}$	-.115713542 $\times 10^{12}$.352371958 $\times 10^{15}$	-.112440499 $\times 10^{18}$.115112932 $\times 10^{20}$
17 \rightarrow 9	.101866743 $\times 10^{-10}$.298198269 $\times 10^{00}$	-.317027836 $\times 10^{04}$.642651194 $\times 10^{07}$	-.683775018 $\times 10^{10}$.409816214 $\times 10^{13}$	-.139691607 $\times 10^{16}$.252730180 $\times 10^{18}$	-.188336946 $\times 10^{20}$
17 \rightarrow 10	.149575136 $\times 10^{-11}$.490441763 $\times 10^{00}$	-.285306551 $\times 10^{04}$.530498798 $\times 10^{07}$	-.550932109 $\times 10^{10}$.328167359 $\times 10^{13}$	-.112072641 $\times 10^{16}$.203964220 $\times 10^{18}$	-.153177379 $\times 10^{20}$
17 \rightarrow 11	.187016697 $\times 10^{-08}$	-.265303999 $\times 10^{00}$	-.120179116 $\times 10^{04}$.306445576 $\times 10^{07}$	-.372382428 $\times 10^{10}$.245788224 $\times 10^{13}$	-.905404407 $\times 10^{15}$.174727171 $\times 10^{18}$	-.137480978 $\times 10^{20}$
17 \rightarrow 12	.430809558 $\times 10^{-08}$	-.332924384 $\times 10^{00}$	-.198293571 $\times 10^{04}$.554577993 $\times 10^{07}$	-.700398763 $\times 10^{10}$.473437344 $\times 10^{13}$	-.177026014 $\times 10^{16}$.344813353 $\times 10^{18}$	-.272869264 $\times 10^{20}$
17 \rightarrow 13	.155079225 $\times 10^{-07}$	-.383577424 $\times 10^{00}$	-.920349385 $\times 10^{03}$.222766072 $\times 10^{07}$	-.265353741 $\times 10^{10}$.174028720 $\times 10^{13}$	-.638418025 $\times 10^{15}$.122657639 $\times 10^{18}$	-.960424342 $\times 10^{19}$
17 \rightarrow 14	.301873489 $\times 10^{-06}$	-.585663901 $\times 10^{00}$.418988126 $\times 10^{03}$	-.953230639 $\times 10^{06}$.113698218 $\times 10^{10}$	-.753005597 $\times 10^{12}$.279065985 $\times 10^{15}$	-.541187804 $\times 10^{17}$.427292716 $\times 10^{19}$
17 \rightarrow 15	.786100247 $\times 10^{-06}$	-.602396882 $\times 10^{00}$.606536265 $\times 10^{03}$	-.144891311 $\times 10^{07}$.176396212 $\times 10^{10}$	-.118288105 $\times 10^{13}$.442075532 $\times 10^{15}$	-.862327541 $\times 10^{17}$.683664229 $\times 10^{19}$
17 \rightarrow 16	.301811507 $\times 10^{-05}$	-.582040058 $\times 10^{00}$.450972790 $\times 10^{03}$	-.107165004 $\times 10^{07}$.130464350 $\times 10^{10}$	-.876394162 $\times 10^{12}$.328277029 $\times 10^{15}$	-.641791505 $\times 10^{17}$.509856336 $\times 10^{19}$